

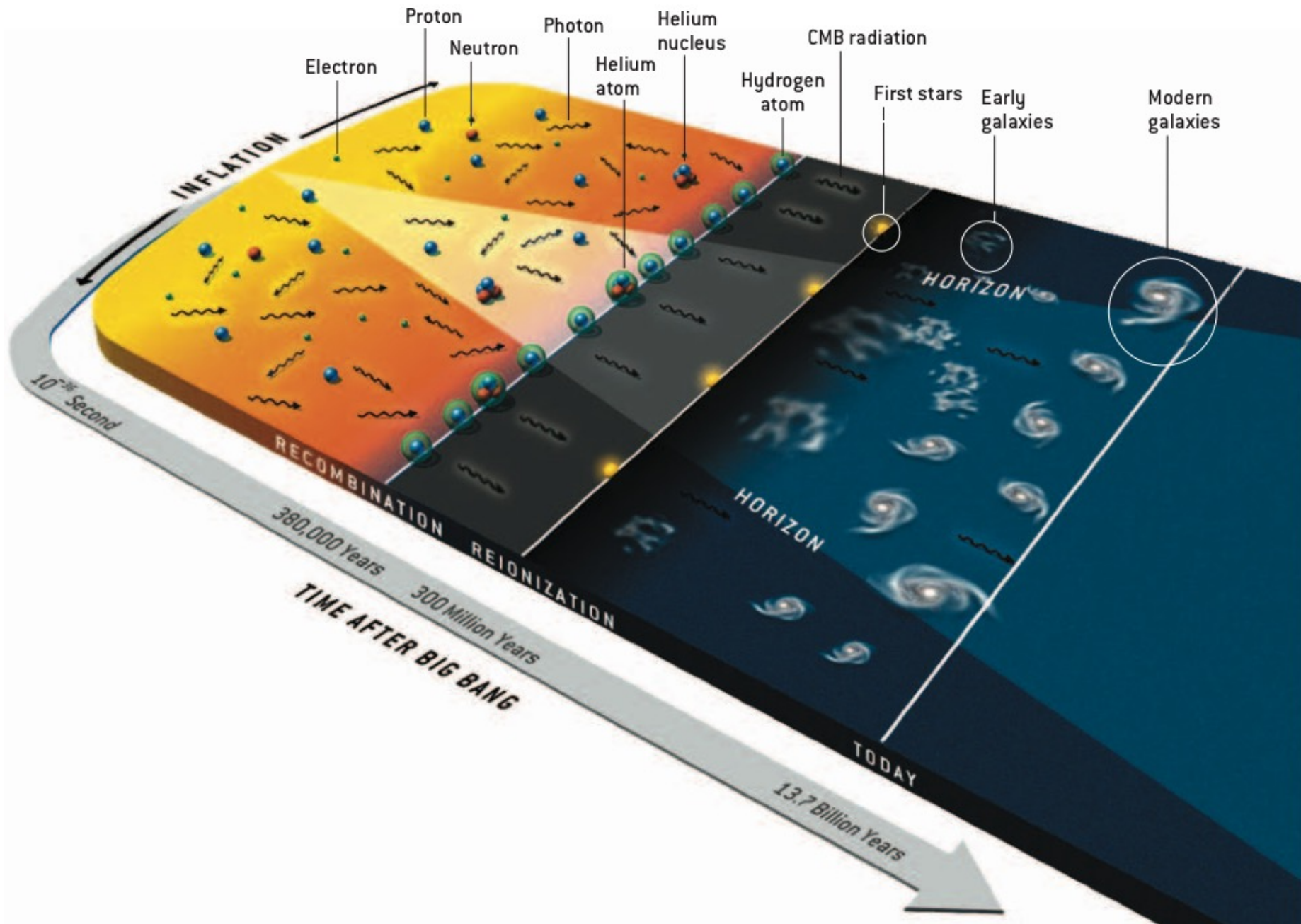
Cosmic Dawn: The First Stars & Galaxies

Alexander Knebe (*Universidad Autonoma de Madrid*)

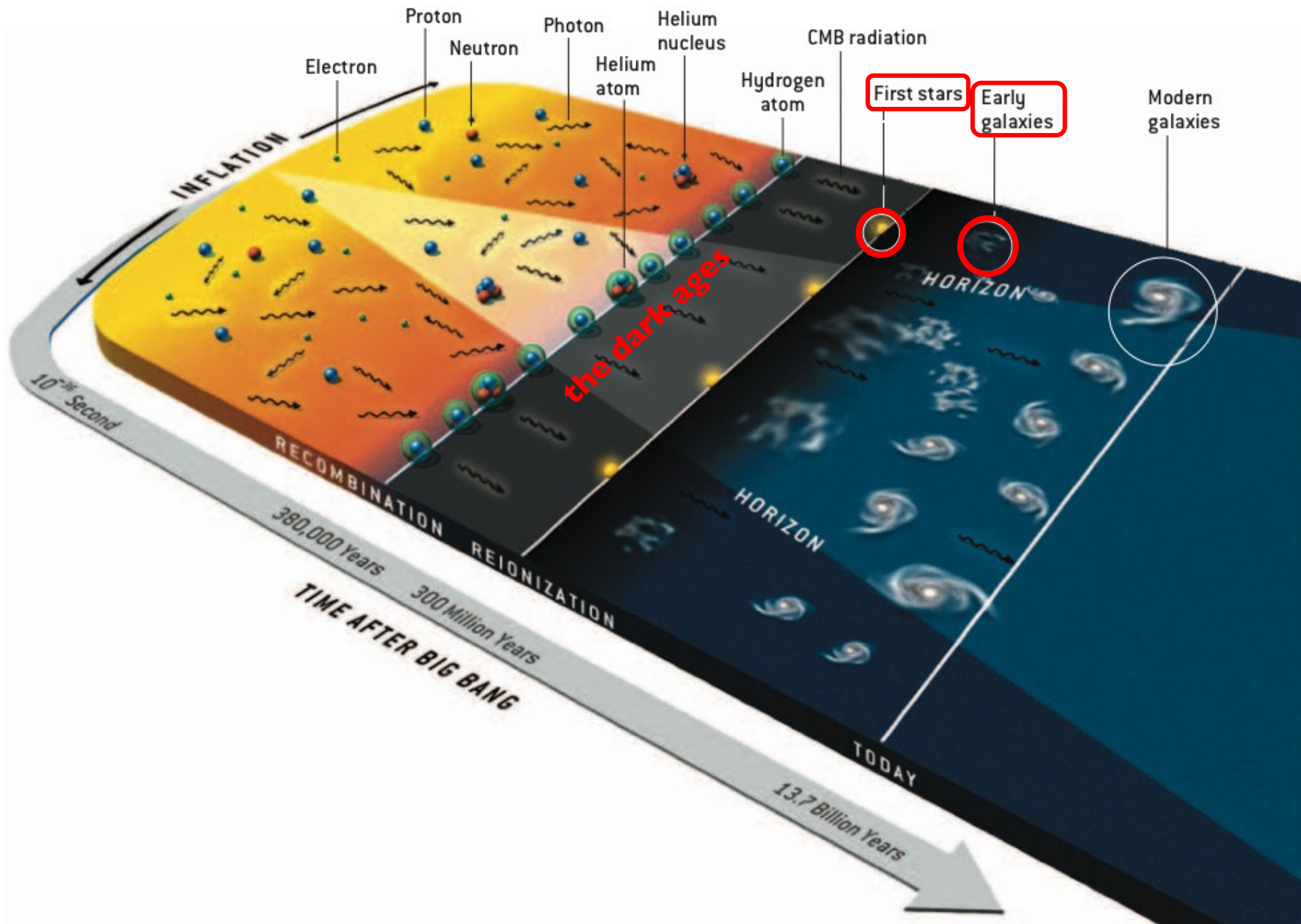


"We've discovered a massive dust and gas cloud which is either the beginning of a new star, or just an awful lot of dust and gas."

Cosmic Dawn: The First Stars & Galaxies



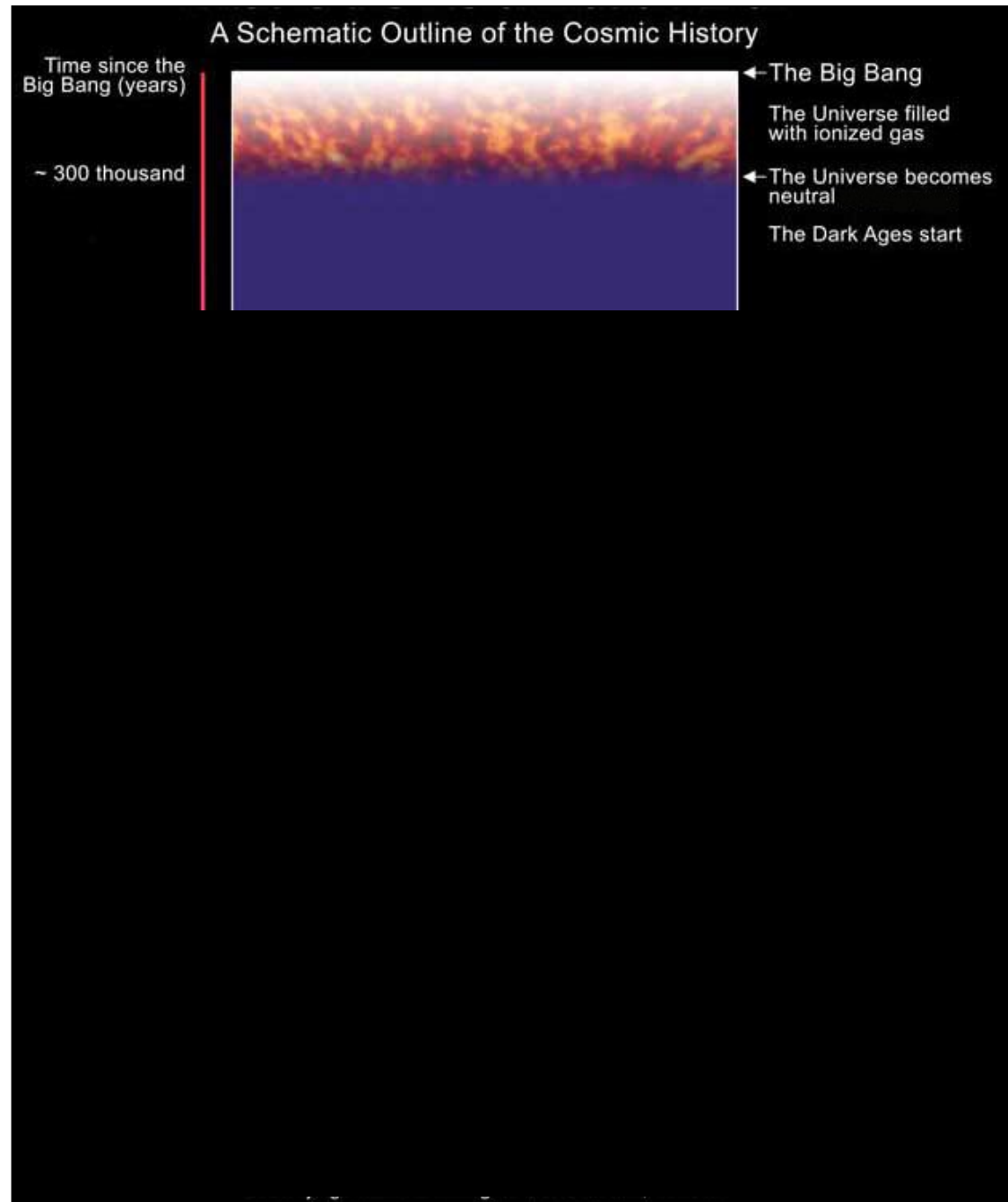
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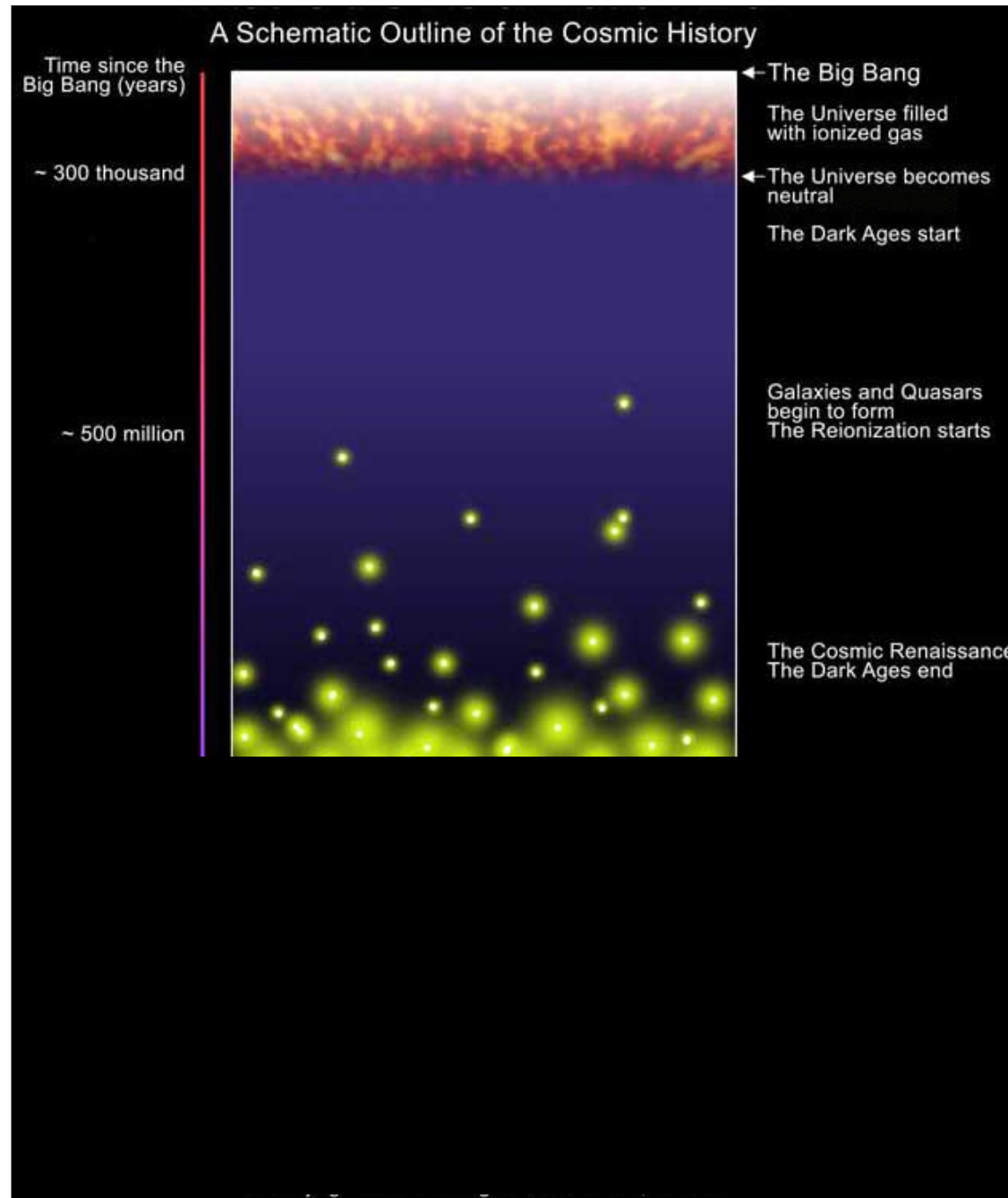


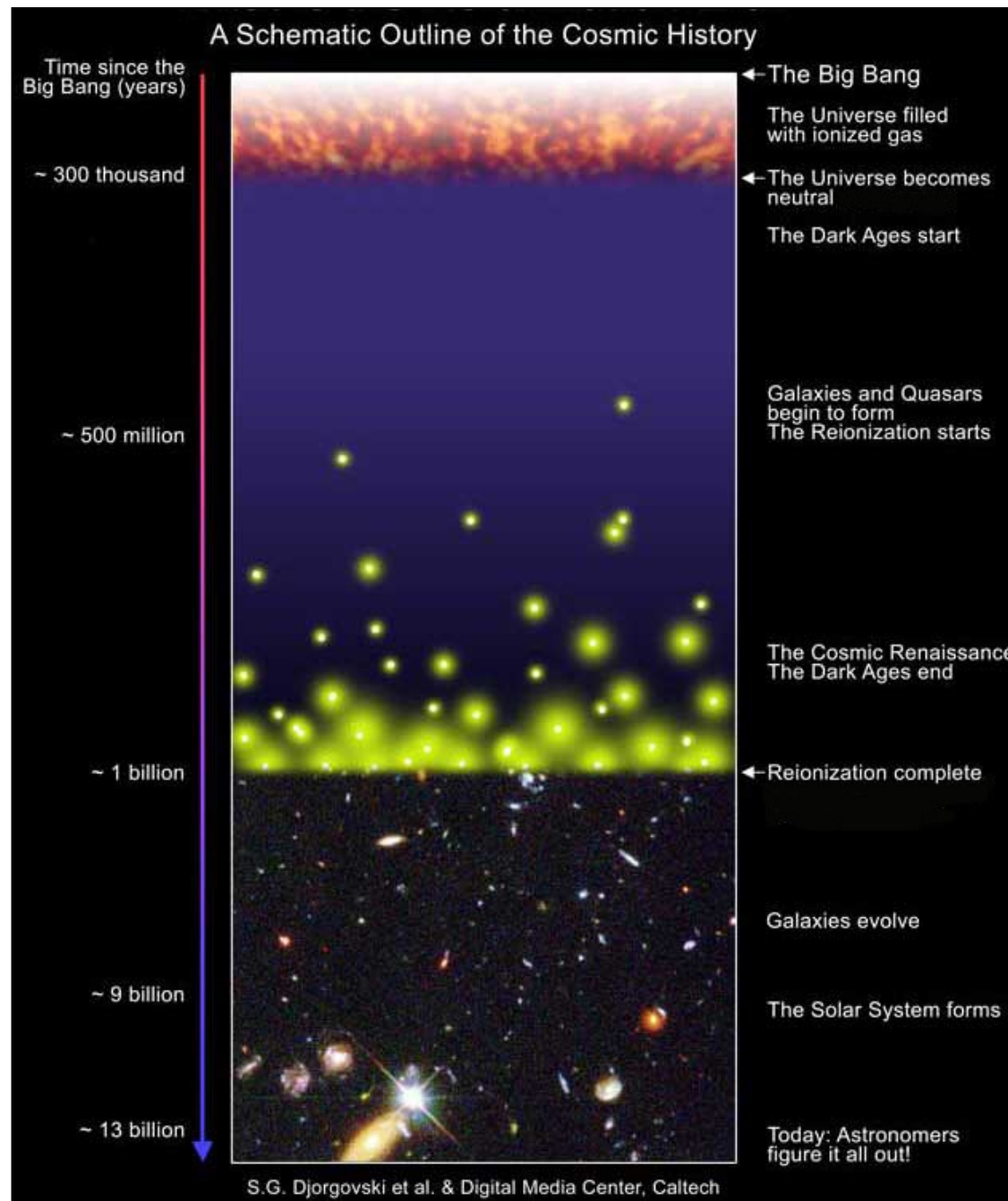
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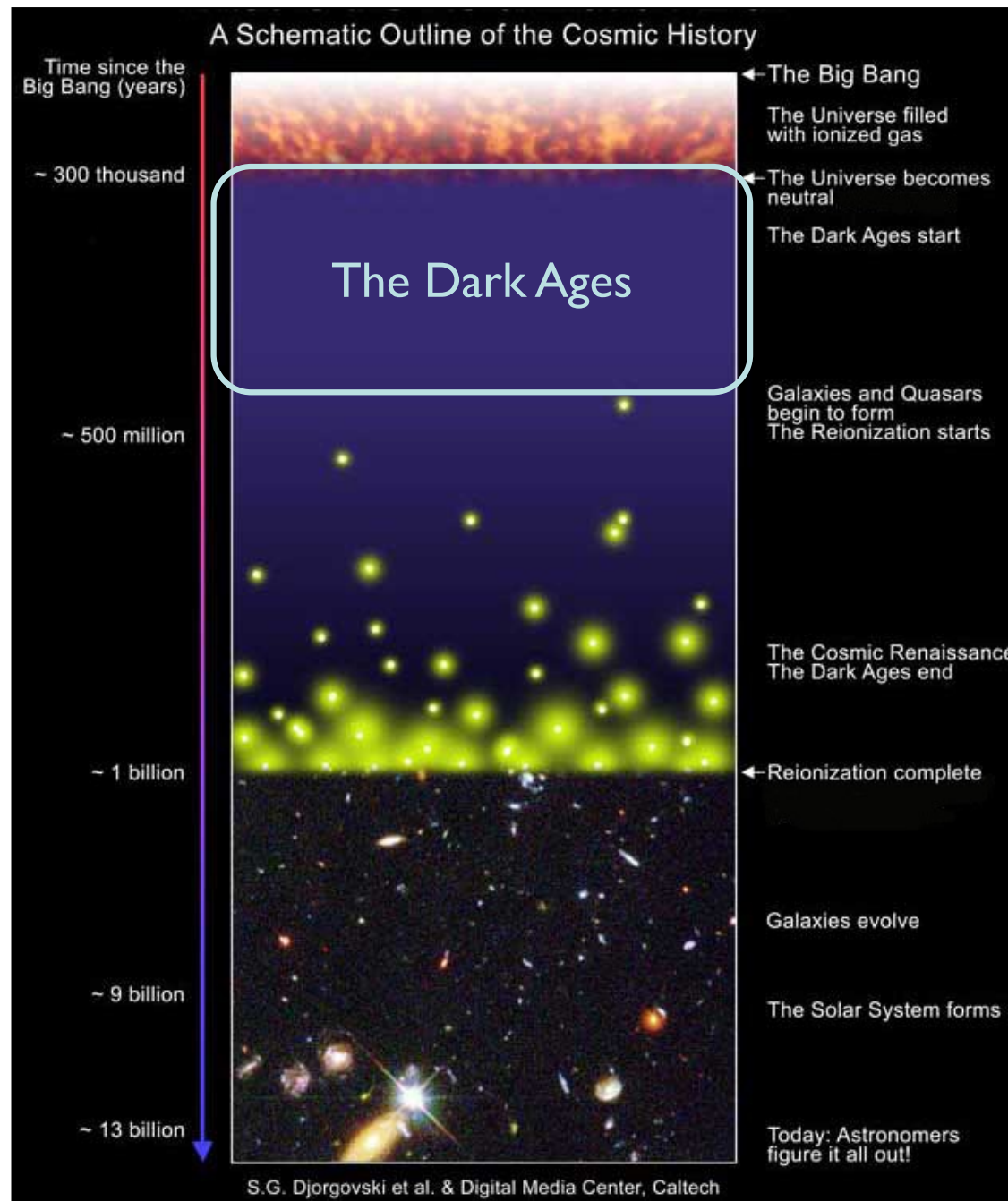
- the dark ages of the Universe
- the first stars
- the first galaxies
- implications for subsequent structure formation

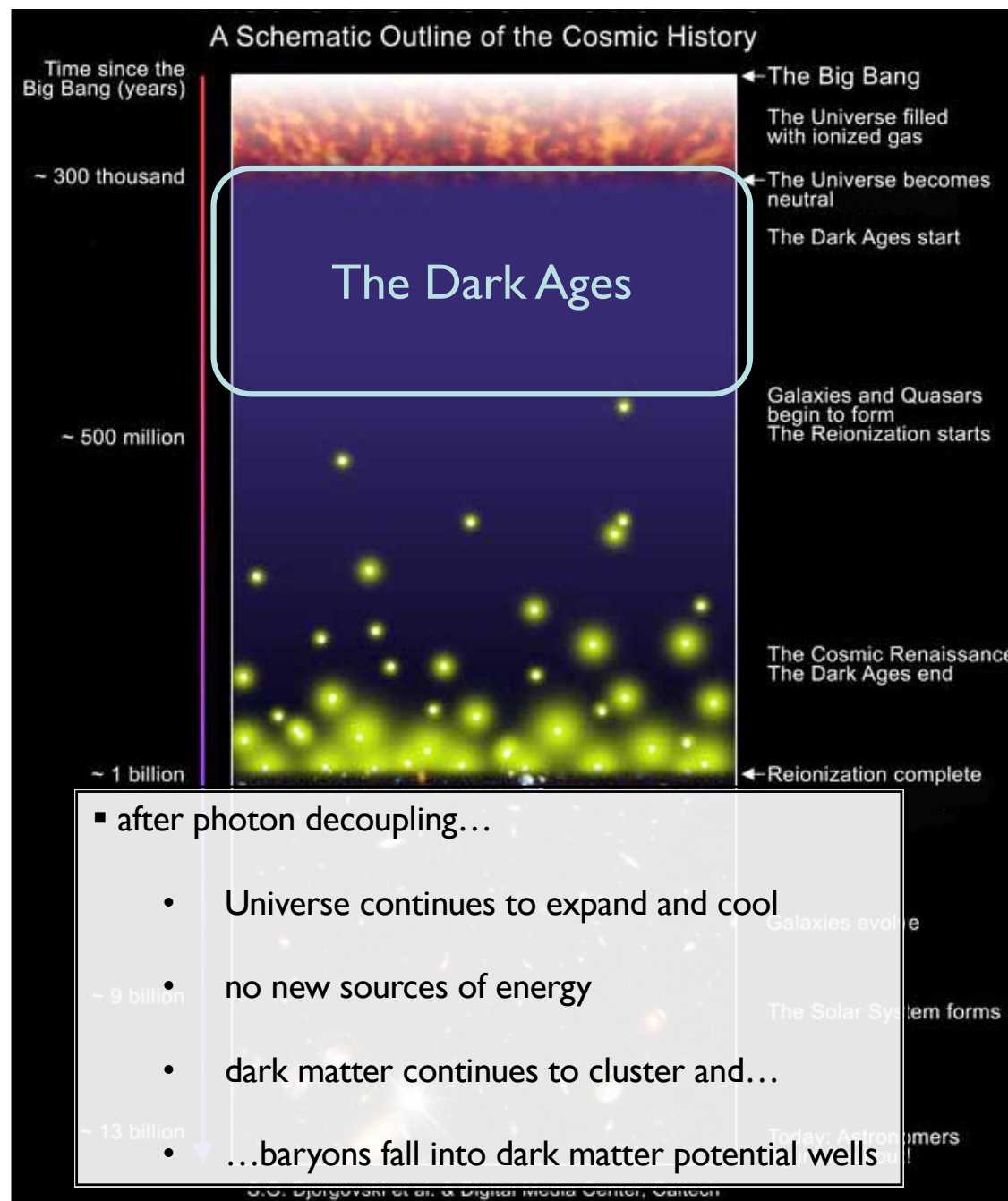
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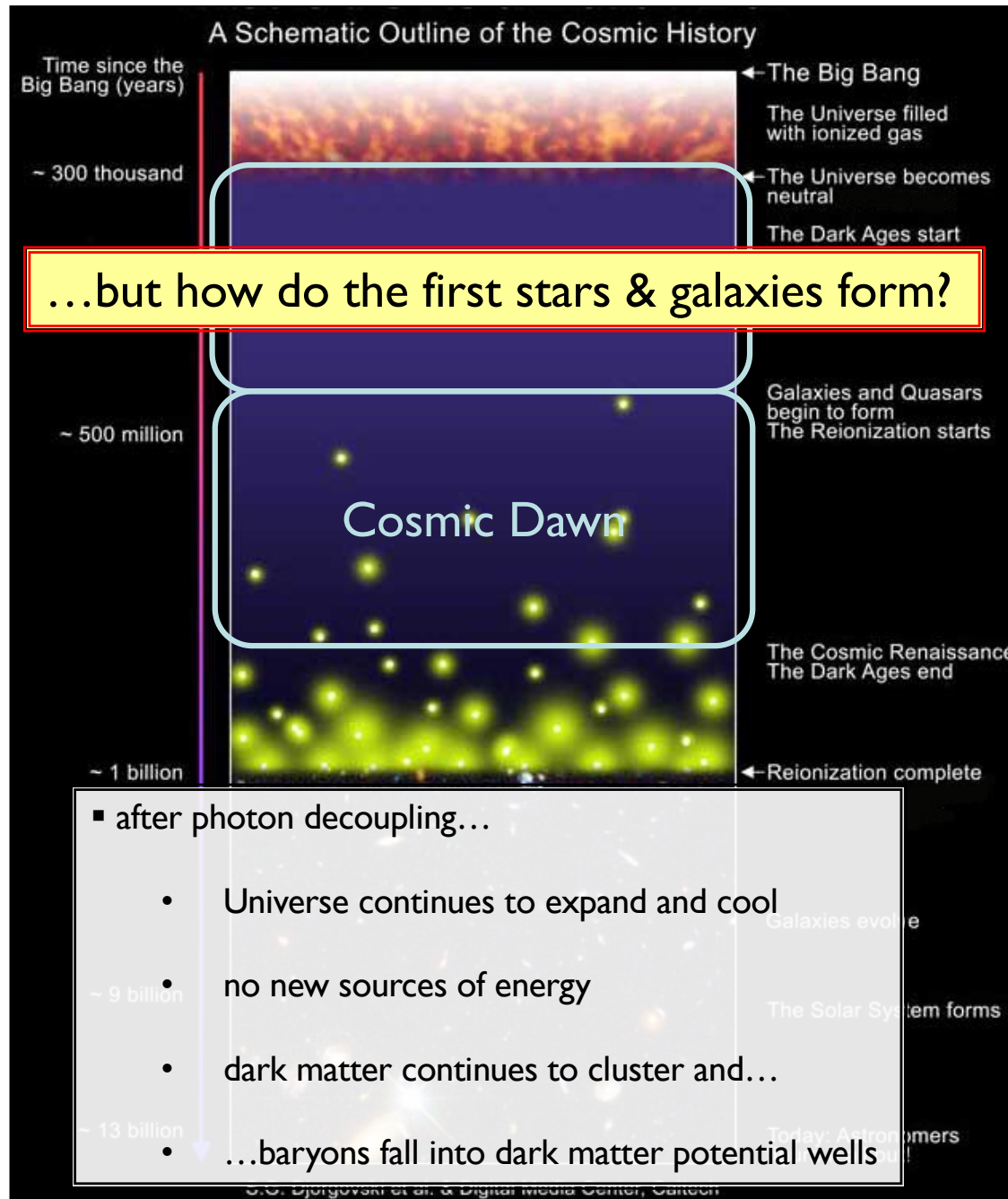












▪ after photon decoupling...

- Universe continues to expand and cool
- no new sources of energy
- dark matter continues to cluster and...

- ...baryons fall into dark matter potential wells

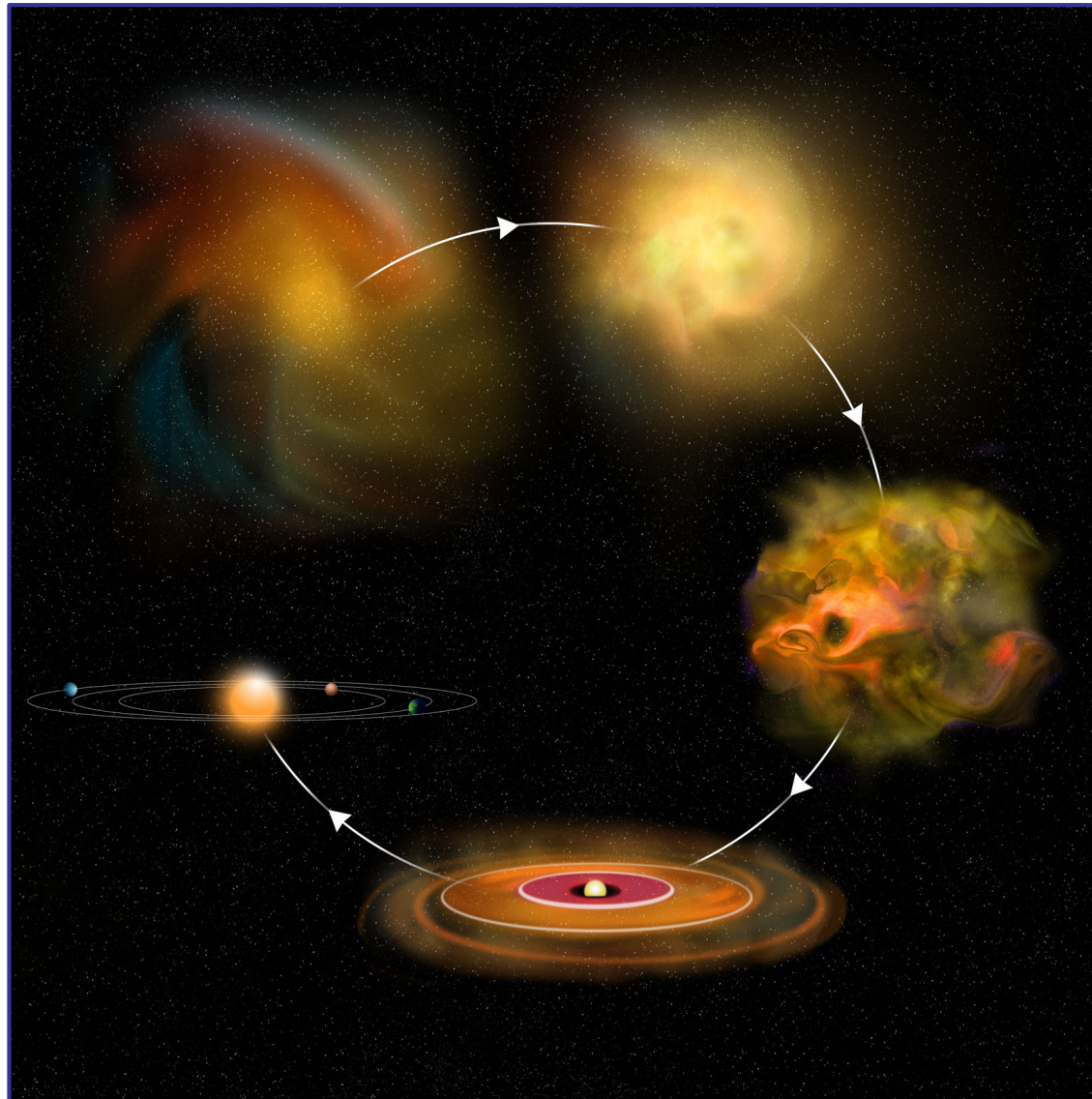
Cosmic Dawn: The First Stars & Galaxies

- the dark ages of the Universe
- **the first stars**
- the first galaxies
- implications for subsequent structure formation

- first stars – summary

- star formation requires coolant for collapse
- only available coolant for first stars = H_2
- sufficient conditions are given for $z < 100$
- numerical models suggest that first stars are very massive $M \in [10, 500]M_{\odot}$
- massive stars die hard & fast:
 - supernovae of $M \in [8, 100]M_{\odot}$ will pollute IGM with metals, and
 - those metals facilitate subsequent star formation

- star formation in general

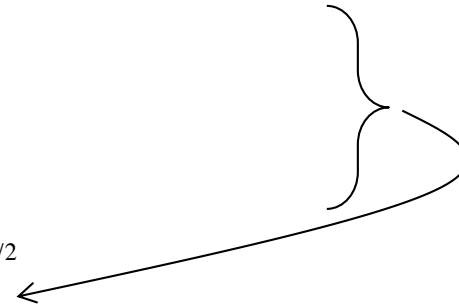


▪ star formation in general

- virial theorem
- energies of homogeneous sphere
- Jeans Mass
- isothermal gravitational collapse
- cooling

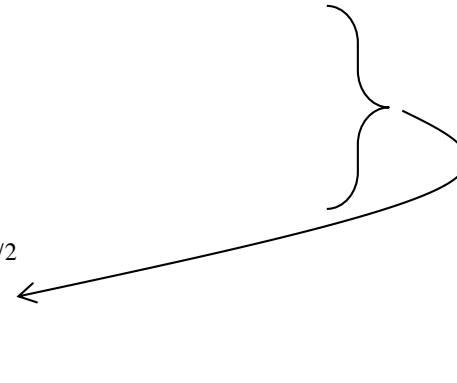
- star formation in general

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- Jeans Mass $M_J = 5.46 \left(\frac{k_B}{G\mu_H m_H} \right)^{3/2} \left(\frac{T^3}{\rho} \right)^{1/2}$
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- cooling



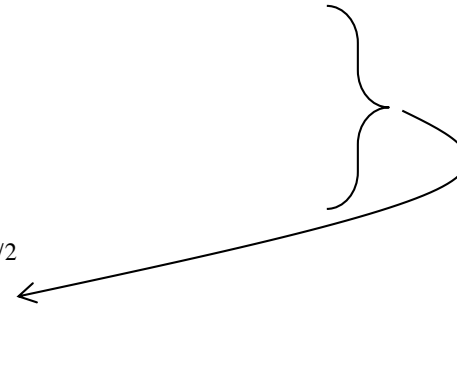
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- star formation in general

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- **isothermal** gravitational collapse
- **cooling!**



- star formation in general

- virial theorem

$$G = \sum_i \vec{p}_i \cdot \vec{r}_i \quad *$$

***Note:** moment of inertia $\Rightarrow I = \sum_i m_i |\vec{r}_i|^2 \Rightarrow \frac{1}{2} \frac{dI}{dt} = \frac{1}{2} \frac{d}{dt} \sum_i m_i |\vec{r}_i|^2 = \frac{1}{2} \sum_i m_i \frac{d|\vec{r}_i|^2}{dt} = \sum_i m_i \frac{d\vec{r}_i}{dt} \cdot \vec{r}_i = \sum_i \vec{p}_i \cdot \vec{r}_i = G$

- star formation in general

- virial theorem

$$\begin{aligned} G = \sum_i \vec{p}_i \cdot \vec{r}_i &\quad \Rightarrow \quad \frac{d}{dt} G = \sum_i \dot{\vec{p}}_i \cdot \vec{r}_i + \sum_i \vec{p}_i \cdot \dot{\vec{r}}_i \\ &= \sum_i \vec{F}_i \cdot \vec{r}_i + \sum_i \vec{p}_i \cdot \dot{\vec{r}}_i \\ &= \sum_i \vec{F}_i \cdot \vec{r}_i + 2 \sum_i E_{kin,i} \\ &= \sum_i \vec{F}_i \cdot \vec{r}_i + 2E_{kin} \end{aligned}$$

- star formation in general

- virial theorem

$$\frac{dG}{dt} = \sum_i \vec{F}_i \cdot \vec{r}_i + 2E_{kin}$$

- star formation in general

- virial theorem

$$\frac{dG}{dt} = \sum_i \vec{F}_i \cdot \vec{r}_i + 2E_{kin}$$



$$\sum_i \vec{F}_i \cdot \vec{r}_i = \sum_i (\nabla E_{pot}) \cdot \vec{r}_i = nE_{pot}$$

$\vec{F} = -\nabla E_{pot}$ $E_{pot} \equiv Cr^n \Rightarrow \nabla E_{pot} = n \frac{E_{pot}}{r} \Rightarrow F \cdot r = nE_{pot}$

- star formation in general

- virial theorem

$$\frac{dG}{dt} = nE_{pot} + 2E_{kin}$$

- star formation in general

- virial theorem

$$\frac{dG}{dt} = nE_{pot} + 2E_{kin}$$

$$\left\langle \frac{dG}{dt} \right\rangle_{\tau} = \frac{1}{\tau} \int_0^{\tau} \frac{dG}{dt} dt = \frac{1}{\tau} [G(\tau) - G(0)]$$

- star formation in general

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↑
bound system!

(coordinates and velocities have upper and lower limits...)

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bound system!
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$$\Rightarrow 0 = \left\langle \frac{dG}{dt} \right\rangle_{\tau} = 2\langle E_{kin} \rangle_{\tau} + n\langle E_{pot} \rangle_{\tau} \quad ; \quad E_{pot} \propto r^n$$

- star formation in general

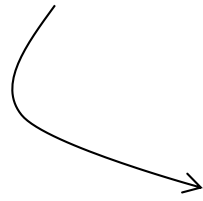
- virial theorem ($n = -1$ for gravity)

$$0 = 2\langle E_{kin} \rangle_{\tau} - \langle E_{pot} \rangle_{\tau} , \quad E_{pot} = Cr^{-1}$$

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can be used to derive the Jeans mass for a homogenous sphere...

- star formation in general

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- gravitational potential of homogeneous sphere (i.e., $\rho = \text{const.}$)

$$M(r) = \rho \frac{4\pi}{3} r^3$$

$$dM(r) = \rho 4\pi r^2 dr$$

$$dE_{pot} = -G \frac{M(r)dM(r)}{r}$$

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$$\begin{aligned} dE_{pot} = -G \frac{M(r)dM(r)}{r} &\quad \Rightarrow \quad E_{pot} = -4\pi G \rho \int_0^R \frac{M(r)}{r} r^2 dr \\ &= -4\pi G \rho^2 \int_0^R \frac{4\pi}{3} r^3 r^2 dr \\ &= -\frac{16\pi^2}{3} G \rho^2 \int_0^R r^4 dr \\ &= -\frac{16\pi^2}{15} G \rho^2 R^5 \\ &= -\frac{16\pi^2}{15} G \frac{M^2}{\left(\frac{4\pi}{3} R^3\right)^2} R^5 \\ &= -\frac{3}{5} G \frac{M^2}{R} \end{aligned}$$

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- virial theorem ($n = -1$ for gravity)

$$0 = 2\langle E_{kin} \rangle_{\tau} - \langle E_{pot} \rangle_{\tau}$$

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$$E_{pot} = -\frac{3}{5}G\frac{M^2}{R} \quad R = \sqrt[3]{\frac{M}{\frac{4\pi}{3}\rho}}$$

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- kinetic energy of homogeneous (gas) sphere

$$E_{kin} = \frac{3}{2}Nk_B T = \frac{3}{2}\frac{M}{\mu_H m_H} k_B T$$

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- kinetic energy of homogeneous (gas) sphere

$$E_{kin} = \frac{3}{2}Nk_B T = \frac{3}{2}\frac{M}{\mu_H m_H} k_B T$$

$$M_J = \sqrt{\frac{3(5k_B)^3}{4\pi(G\mu_H m_H)^3}} \sqrt{T^3} \frac{1}{\sqrt{\rho}}$$

- star formation in general

- virial theorem ($n = -1$ for gravity)

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- Jeans mass

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relation between T and ρ determines fate of collapse...

- star formation in general
 - nature of gravitational collapse
= adiabatic?

- star formation in general

- nature of gravitational collapse

= adiabatic?

$$PV^\gamma = \text{const.} \Rightarrow T \propto \rho^{\gamma-1} \Rightarrow T \propto \rho^{2/3}$$

$$P = \frac{\rho}{\mu_H m_H} k_B T$$

$$\gamma = 5/3$$

(monatomic gas)

- star formation in general

- nature of gravitational collapse

= adiabatic?

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$$P = \frac{\rho}{\mu_H m_H} k_B T \quad \gamma = 5/3 \quad (\text{monatomic gas})$$



$$M_J = 5.46 \left(\frac{k_B}{G \mu_H m_H} \right)^{3/2} \left(\frac{T^3}{\rho} \right)^{1/2} \propto \sqrt{\rho}$$

$M > M_J \Rightarrow$ collapse starts $\Rightarrow \rho \nearrow \Rightarrow M_J \nearrow \Rightarrow$ collapse **stops!**

- star formation in general
 - nature of gravitational collapse
= isothermal?

- star formation in general
 - nature of gravitational collapse
= isothermal!

$$T = \text{const.}$$



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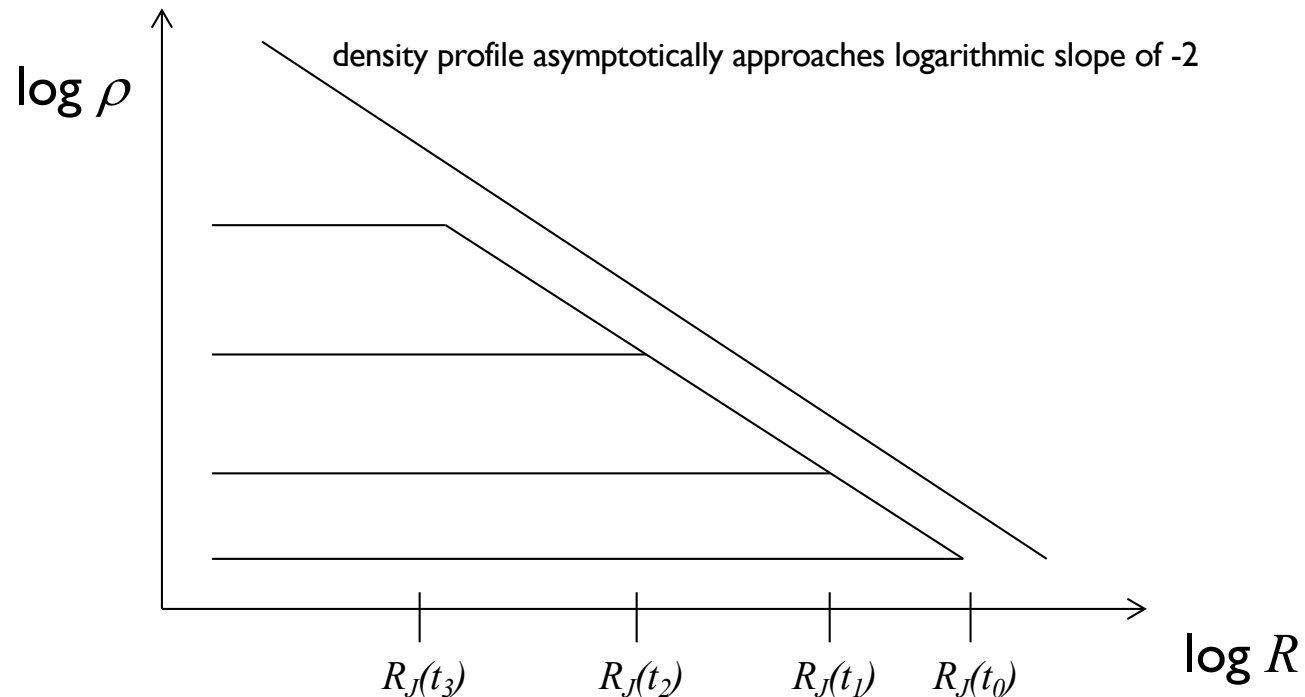


$M > M_J \Rightarrow$ collapse starts $\Rightarrow \rho \nearrow \Rightarrow M_J \searrow \Rightarrow$ “runaway” collapse!

collapse converges to **isothermal sphere...**

- star formation in general
 - nature of gravitational collapse
 - = isothermal sphere

$$\rho \propto \frac{M_J}{R_J^3} \propto \frac{1/\sqrt{\rho}}{R_J^3} \Rightarrow \rho^{3/2} \propto \frac{1}{R_J^3} \Rightarrow \rho \propto \frac{1}{R_J^2} \Rightarrow \log \rho \propto -2 \log R$$



- star formation in general

- nature of gravitational collapse

= isothermal collapse **requires cooling:**

dust grains/metals can absorb and re-emit energy...
...but there are no such things at cosmic dawn!?*

▪ star formation in general

- nature of gravitational collapse

= isothermal collapse **requires cooling:**

dust grains/metals can absorb and re-emit energy...
...but there are no such things at cosmic dawn!?

this is where and why the first star formation differs from today's:
in the primeval Universe was no dust/metal acting as coolant!

- first star formation

- cooling

the dominant coolant is (molecular) hydrogen H_2 !

▪ first star formation

• cooling

the dominant coolant is (molecular) hydrogen H_2 !

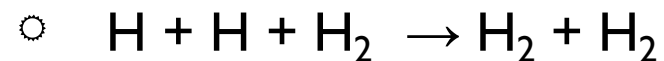
• cooling by H_2 via rotational/vibrational channels:

- rotational/vibrational excitation through collision
- de-excitation via...
 - radiation (\rightarrow cooling) or
 - collision

▪ first star formation

- cooling by H_2 requires H_2 in the first place...

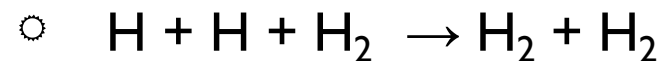
∴ formation of H_2



- first star formation

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∴ formation of H_2



we require*:

- presence of free e and p

*remnants of the epoch of recombination plus ionized H by energy of initial collapse

- first star formation

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we require*:

- presence of free e and p

- high densities $n_H > 10^8 \text{cm}^{-3}$

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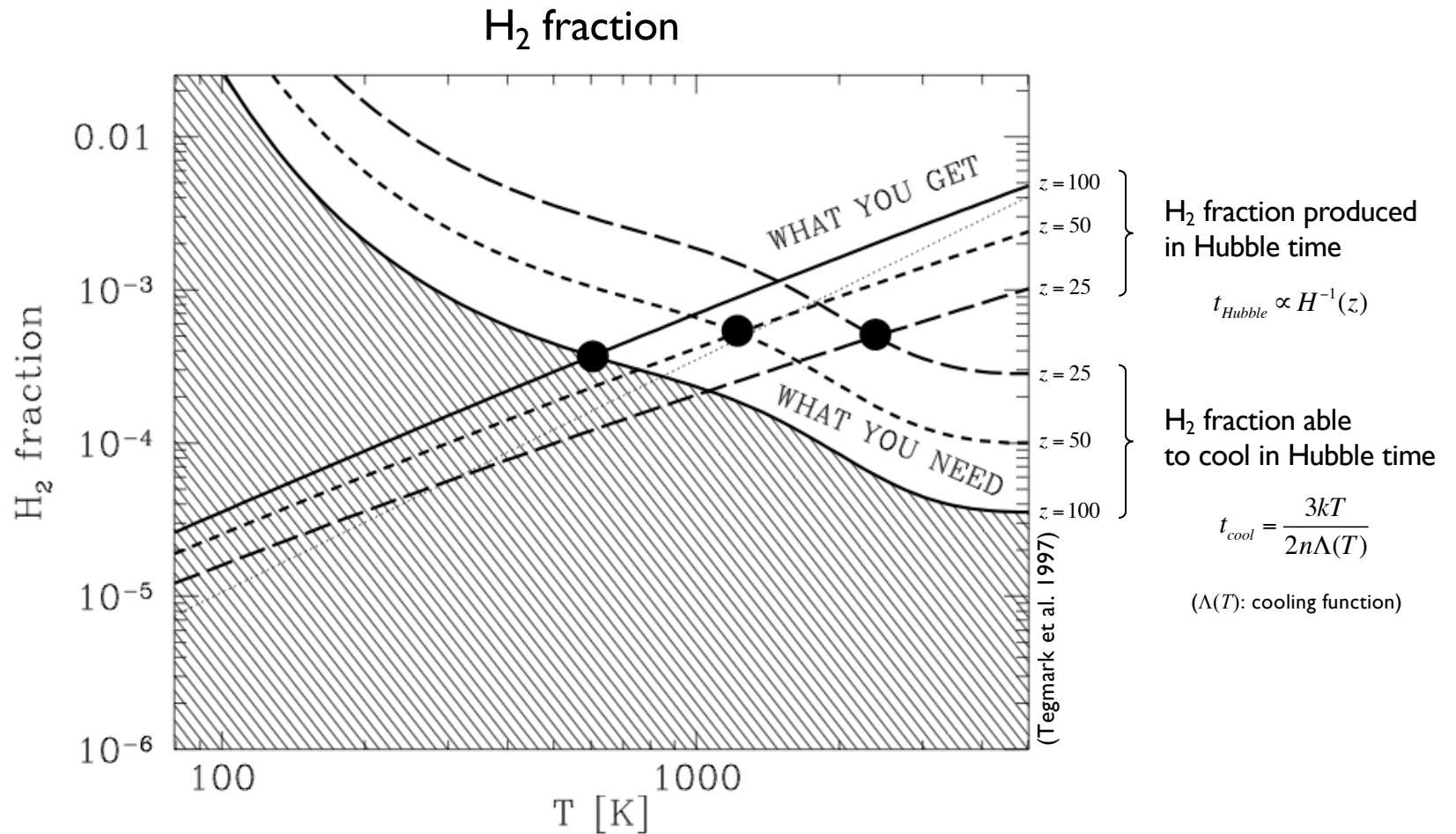
∴ formation of H_2 requires:

- presence of free e and p
- high densities $n_{\text{H}} > 10^8 \text{cm}^{-3}$

∴ H_2 fraction χ_{H_2} must exceed $\sim 5 \times 10^{-3}$ for cooling to be effective

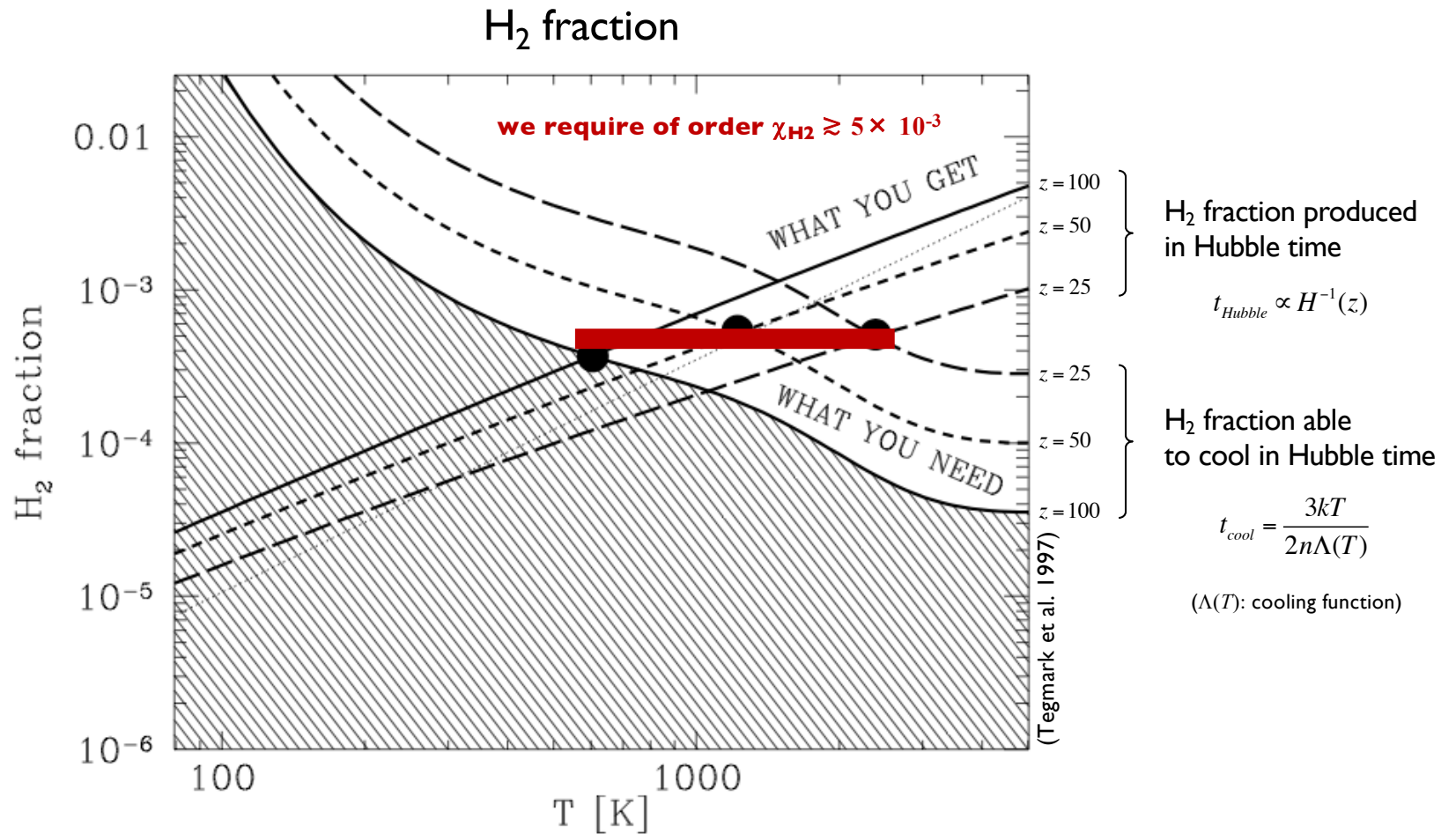
▪ first star formation

- cooling by H_2 : *formation of H_2*



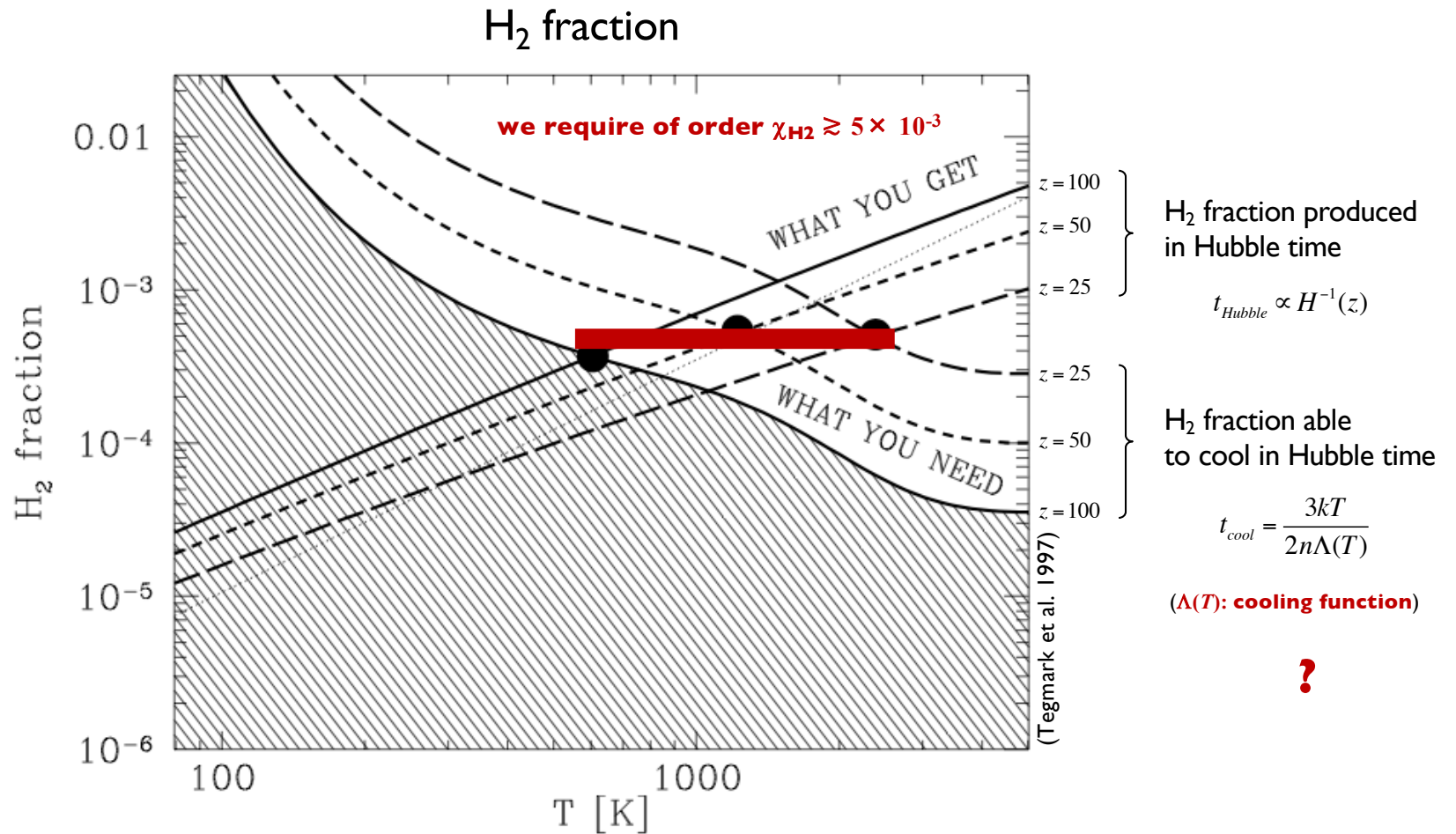
▪ first star formation

- cooling by H₂: *formation of H₂*



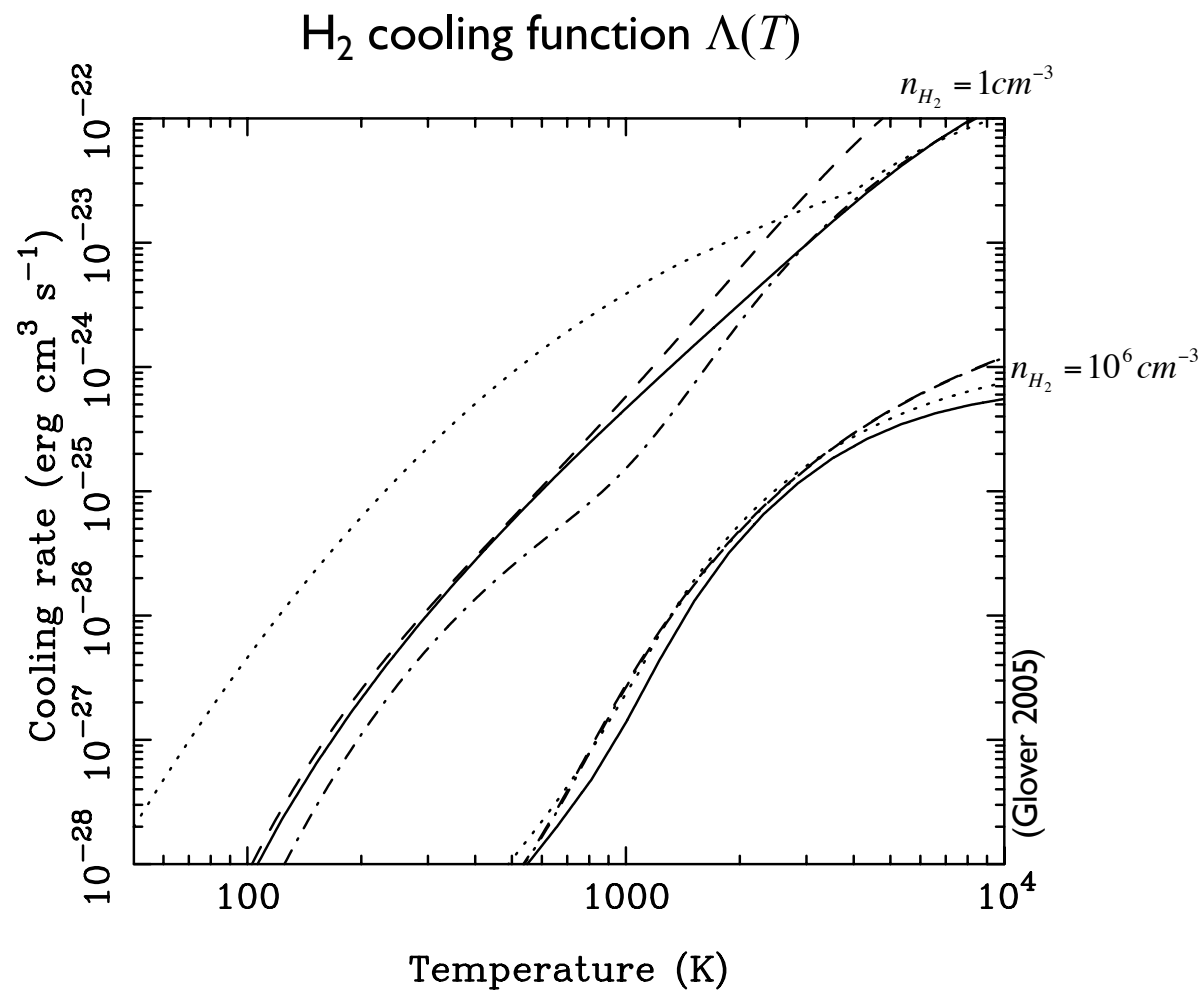
▪ first star formation

- cooling by H₂: formation of H₂



■ first star formation

- cooling by H_2 : *formation of H_2*



cooling efficiency increases with temperature! →

▪ first star formation

• cooling by H₂

- adiabatic collapse due to lack of sufficient H₂
- increasing density leads to more H₂
- increasing temperature leads to more efficient cooling
- collapse becomes isothermal...

▪ first star formation

• cooling by H₂

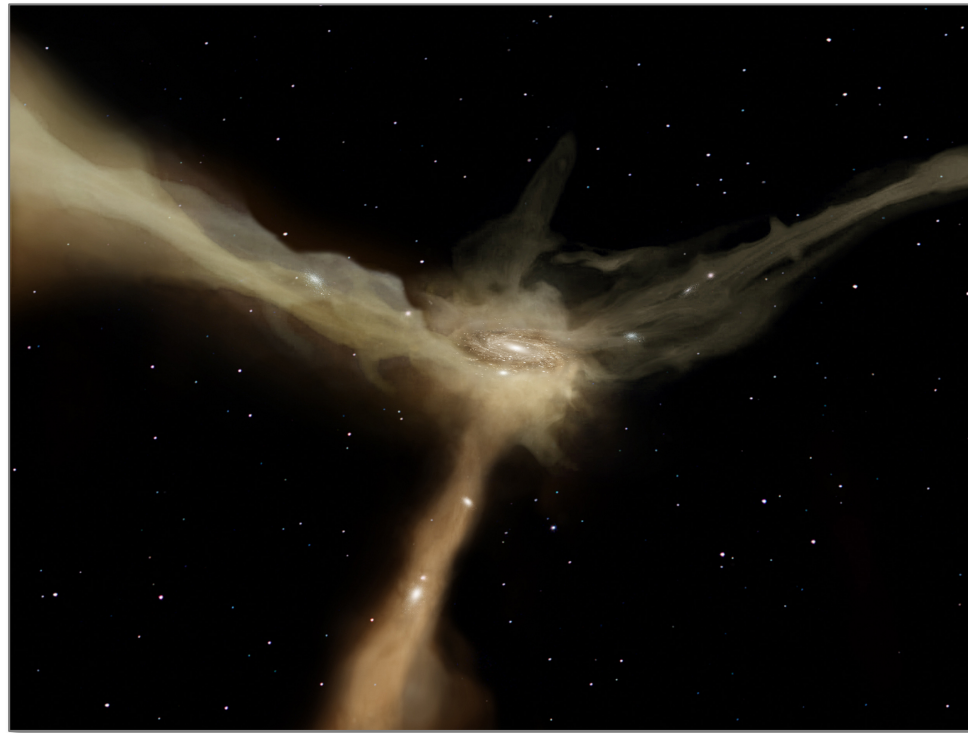
- adiabatic collapse due to lack of sufficient H₂
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...how massive are those first stars?

- first star formation

- masses of first stars

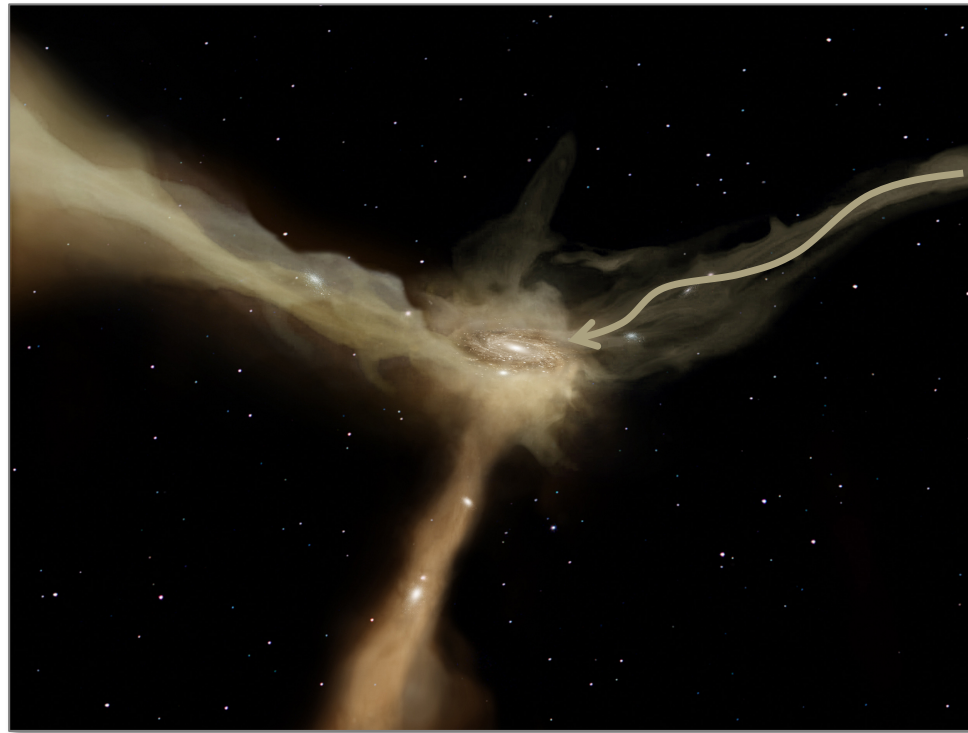
- mass growth of proto-stellar gas cloud: $M_*(t) = M_{pr} + \int_0^t \dot{M}(\tau) d\tau$



- first star formation

- masses of first stars

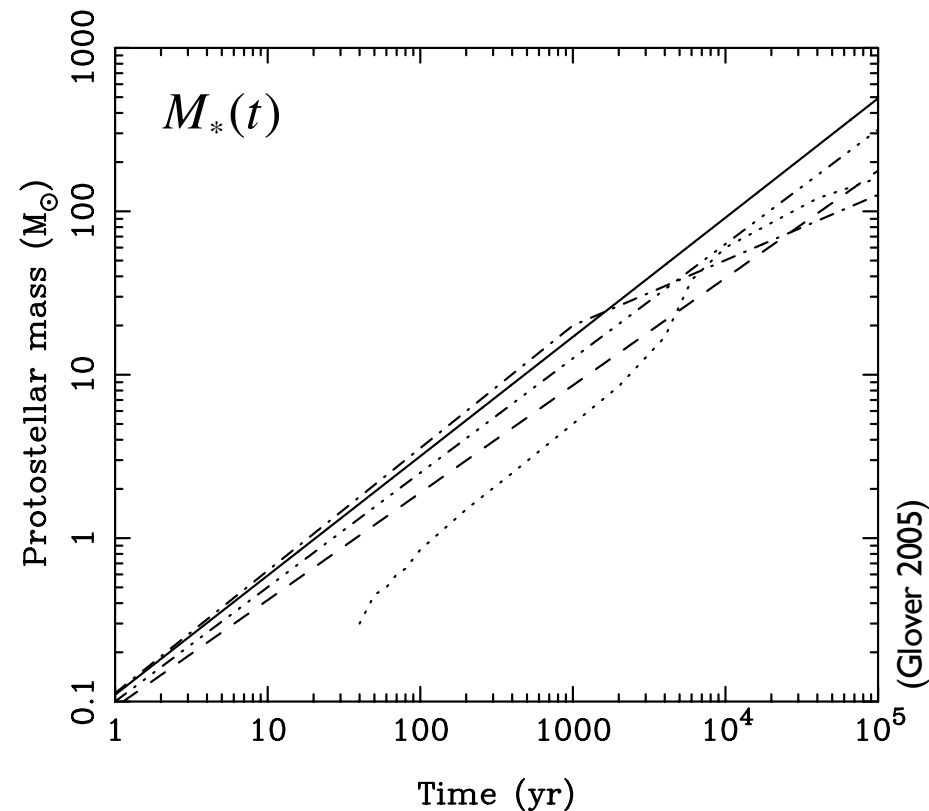
- mass growth of proto-stellar gas cloud: $M_*(t) = M_{pr} + \int_0^t \dot{M}(\tau) d\tau$
 $\dot{M} = dM/dt$



- first star formation

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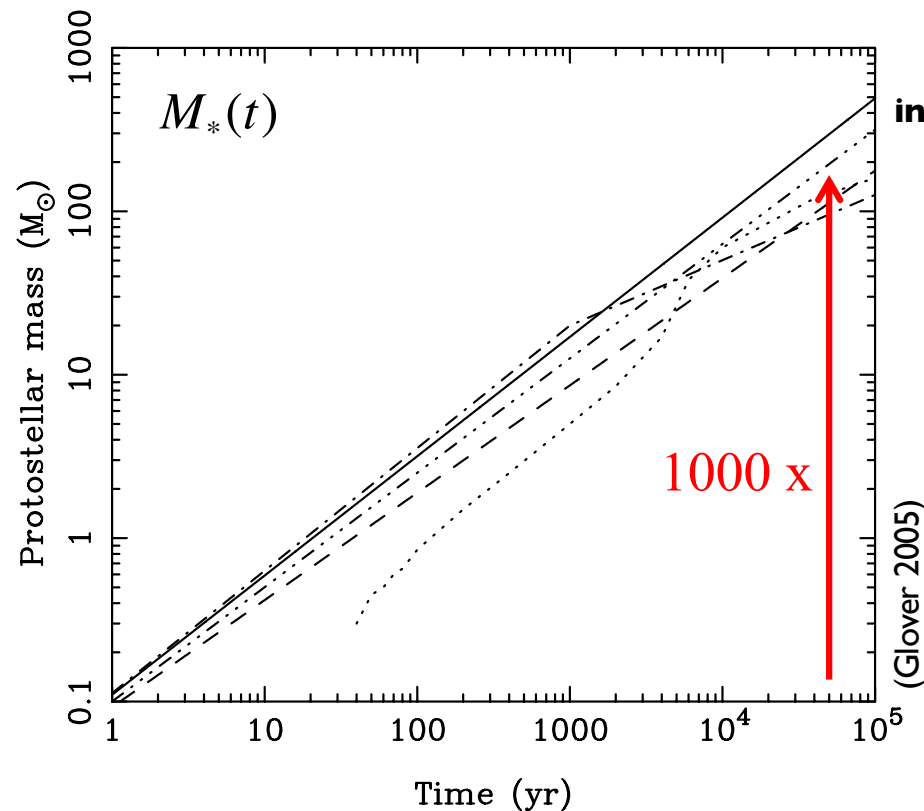
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- numerical models for mass accretion rate $\dot{M} = dM/dt$ lead to...



- first star formation

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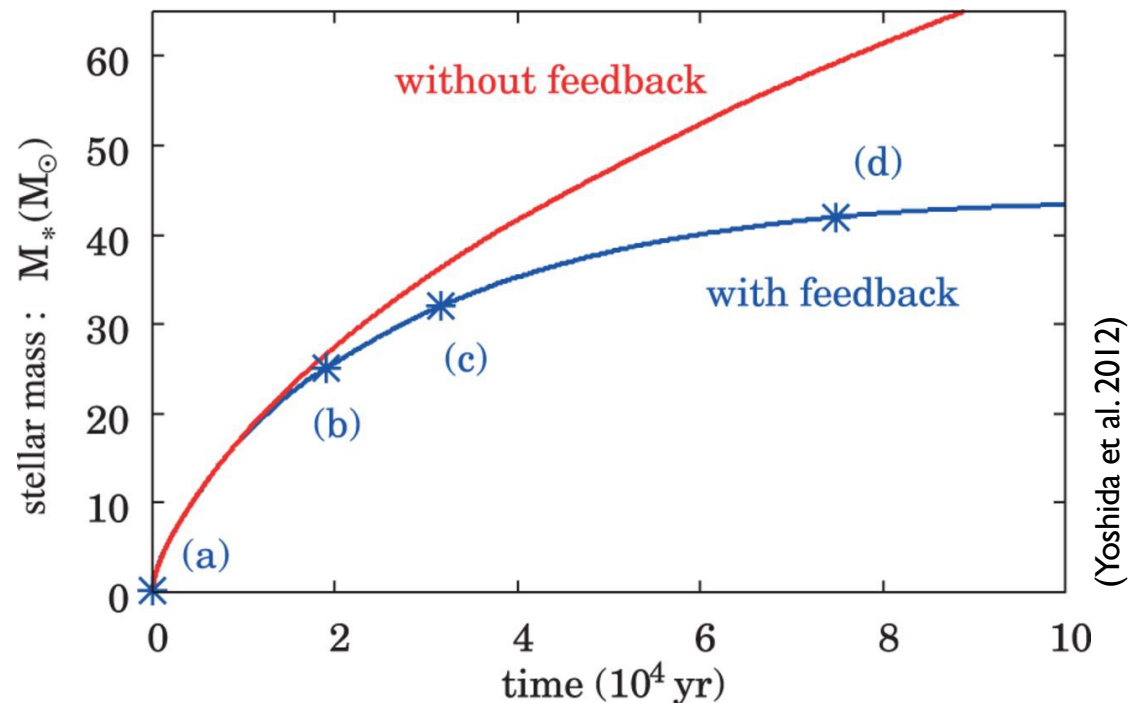


in very short times the proto-star becomes extremely massive!

- first star formation

- masses of first stars

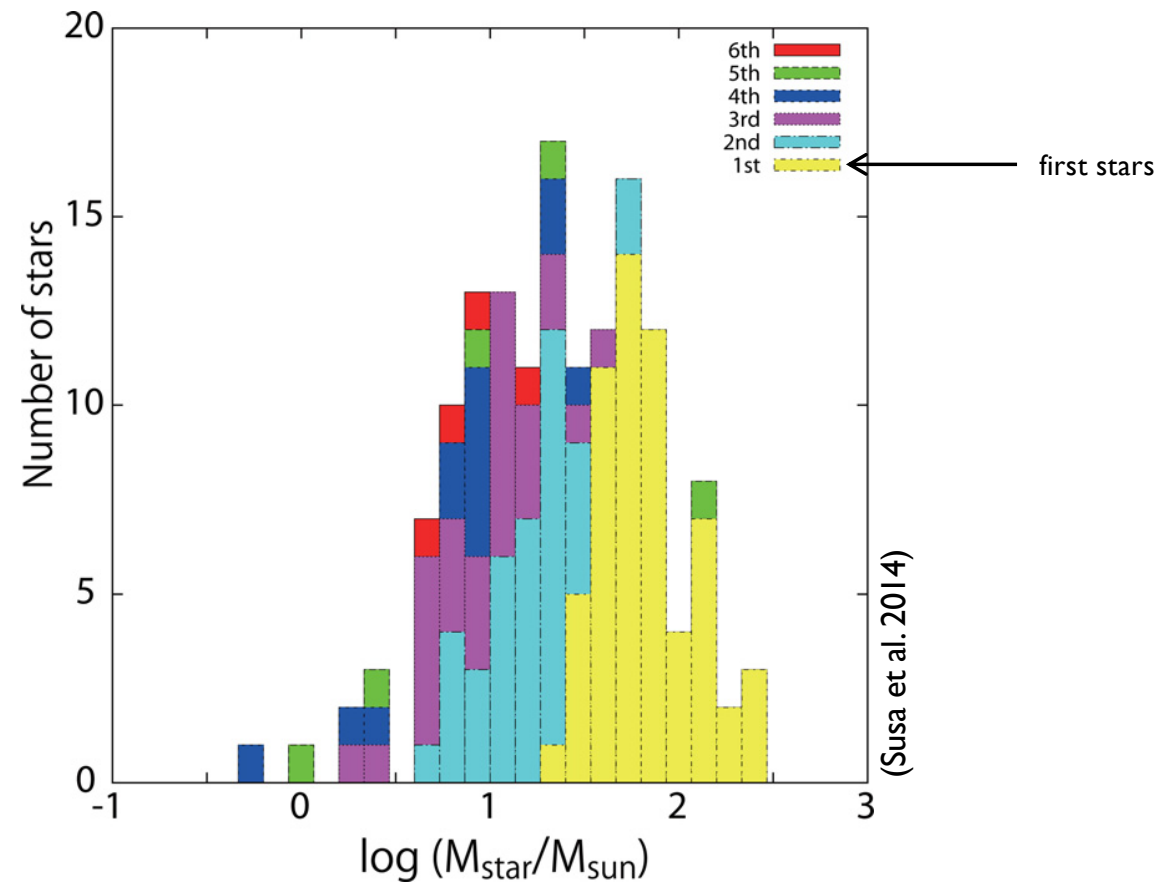
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- feedback can substantially reduce accretion rates and hence M_* :



- first star formation

- primeval Initial Mass Function

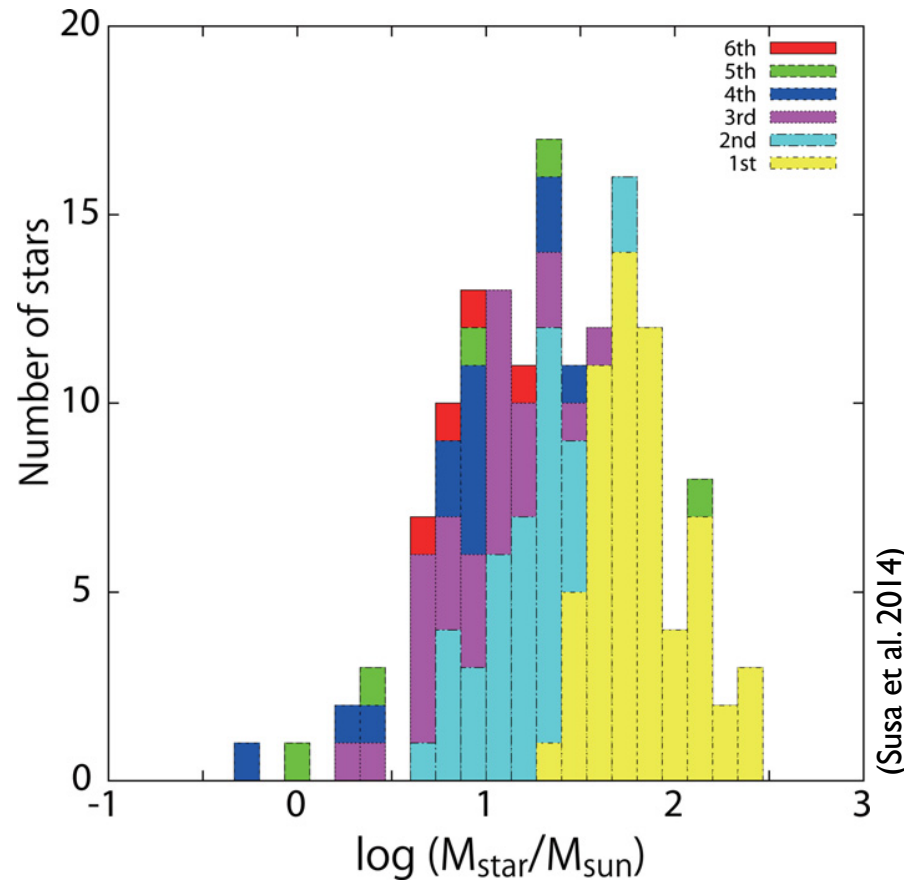
- first stars have mass $M \in [10, 500]M_{\odot}$
- determined via simulations:



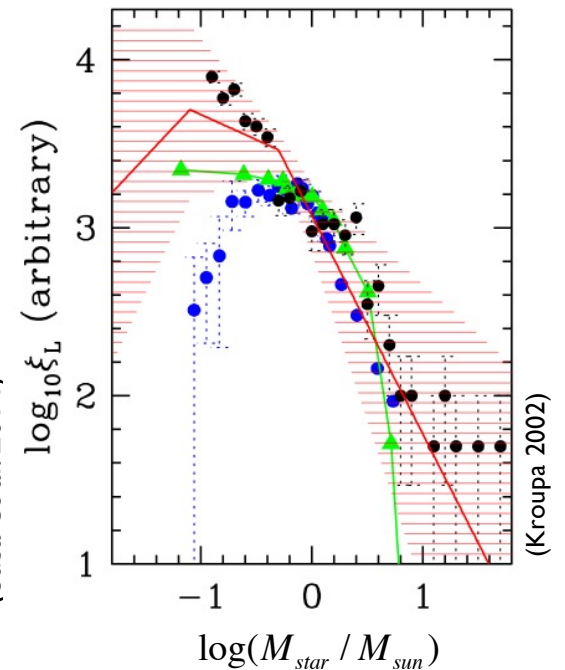
- first star formation

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substantially different from current IMF:



- on the life and death of high-mass stars

- mass-luminosity relation for main sequence stars

$$L \propto \frac{dE}{dt}$$

- on the life and death of high-mass stars

- mass-luminosity relation for main sequence stars*

$$L \propto \frac{dE}{dt} \propto M^{3.5}$$

*approximate derivation:

perfect black-body radiator: $L = 4\pi R^2 \sigma T^4$

hydrostatic equilibrium: $\frac{dP}{dr} = -\frac{GM\rho}{r^2} \Rightarrow \langle P \rangle = -\frac{1}{3} \frac{E_{pot}}{V} \Rightarrow \langle P \rangle V = -\frac{1}{3} E_{pot} = \frac{1}{5} \frac{GM^2}{R} = NkT = \frac{M}{m_H} kT = \frac{M}{m_H} k \frac{L^{1/4}}{4\pi R^{1/2}}$

$$M^{3.33} \propto L \leftarrow M^4 \propto L M^{2/3} \xleftarrow{R \propto M^{1/3}} M^4 \propto L R^2 \leftarrow M \propto L^{1/4} R^{1/2} \leftarrow \frac{M^2}{R} \propto M \frac{L^{1/4}}{R^{1/2}}$$

- on the life and death of high-mass stars

- mass-luminosity relation for main sequence stars

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$$E \propto M$$

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$$E \propto M$$

→ typical time on main sequence $\tau = E/L \propto M^{-2.5}$

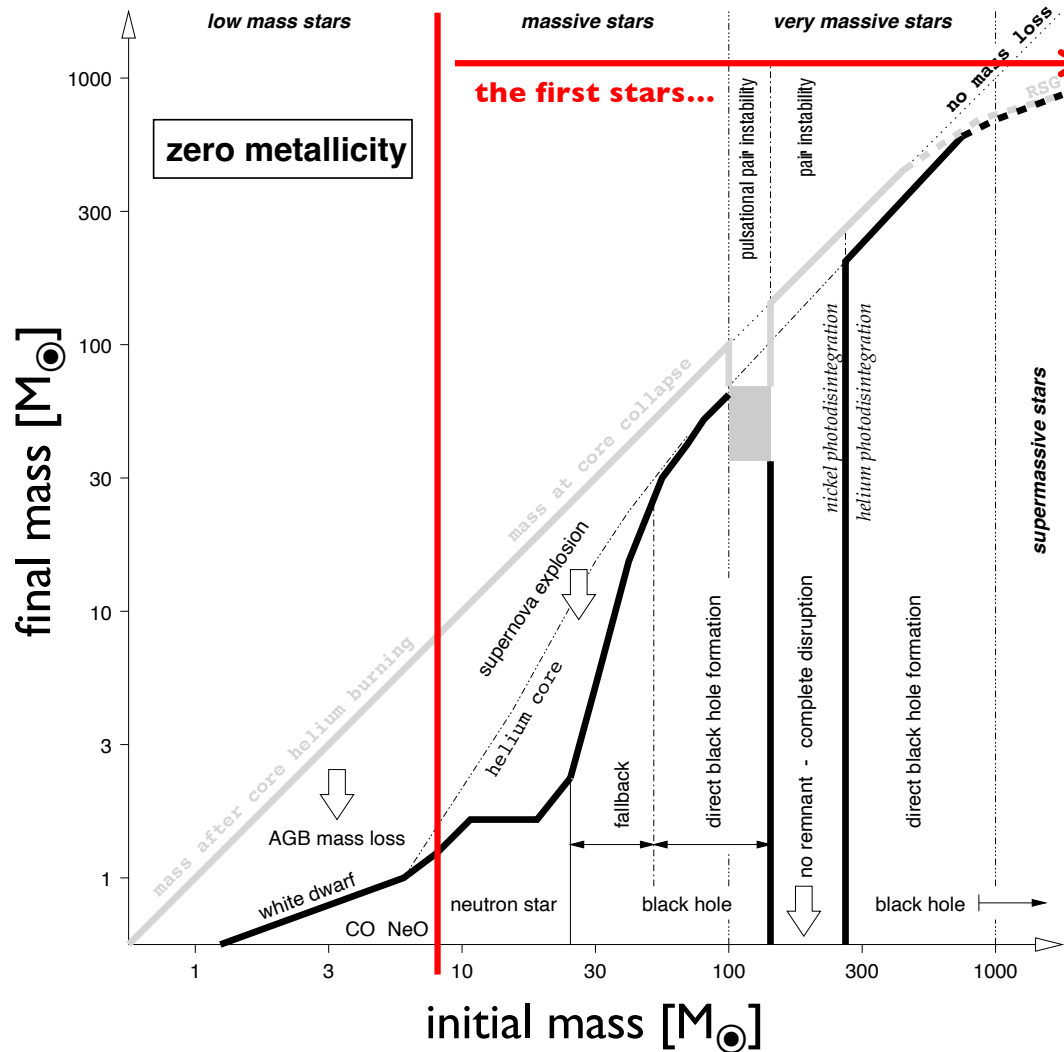
high-mass stars die hard[§] & fast*

[§] spectacular end-stages

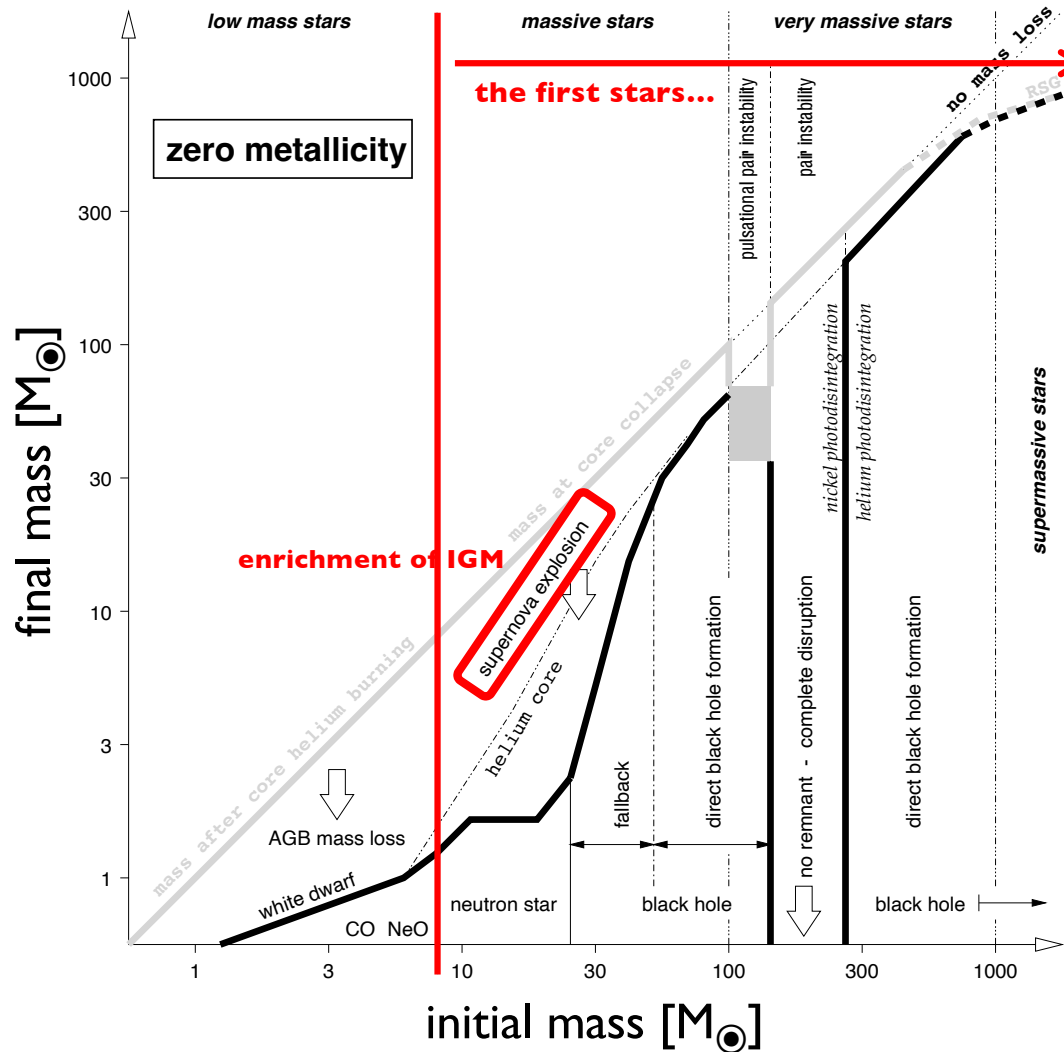
*after a few Myrs only!

- on the life and death of high-mass stars
 - metal-free high-mass stars either...
 - form a black hole or...
 - completely disrupt ('pair instability supernova')

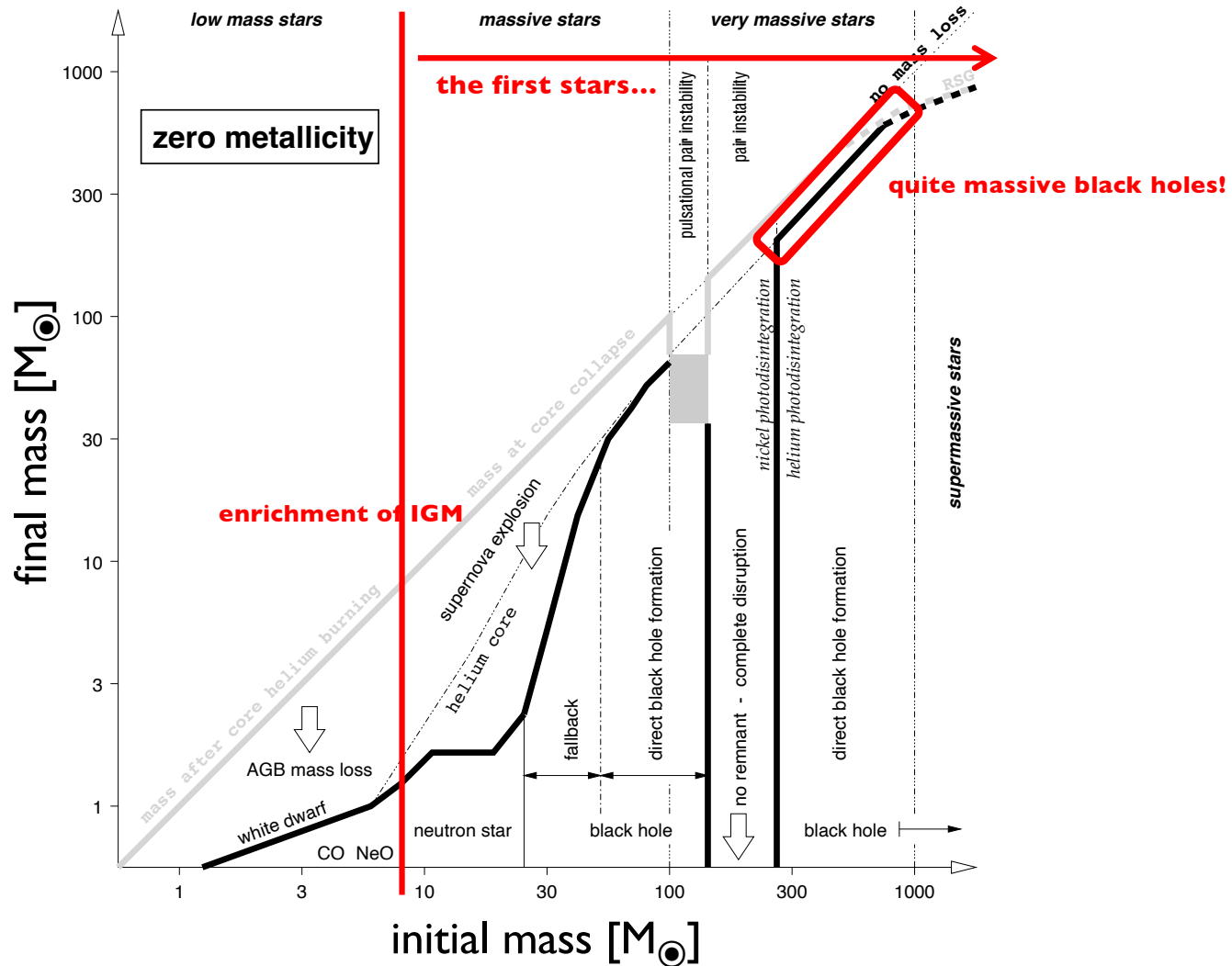
- on the life and death of high-mass stars
 - initial mass vs. final mass in general



- on the life and death of high-mass stars
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- on the life and death of high-mass stars
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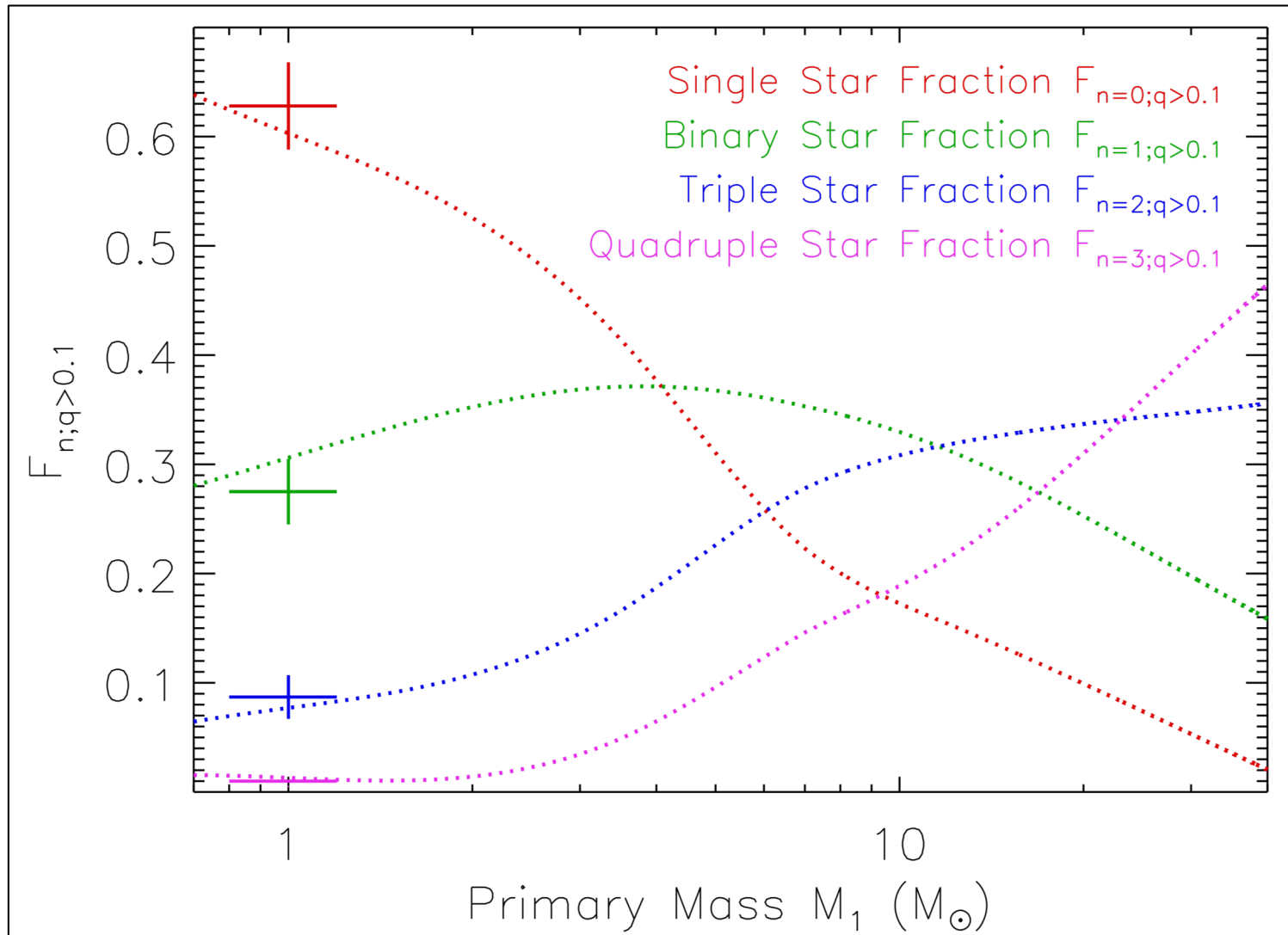
▪ first stars – summary

- star formation requires coolant for collapse
- only available coolant for first stars = H_2
- sufficient conditions are given for $z < 100$
- numerical models suggest that first stars are very massive $M \in [10, 500]M_\odot$
- massive stars die hard & fast:
 - supernovae of $M \in [8, 100]M_\odot$ will pollute IGM with metals, and
 - those metals facilitate subsequent star formation

- first stars – open questions
 - do the first stars also form in binaries?
 - how did Pop III star formation come to an end?
 - what is the influence of magnetic fields?
 - how exactly works turbulence/fragmentation?
 - what about dark matter?

- first stars – open questions

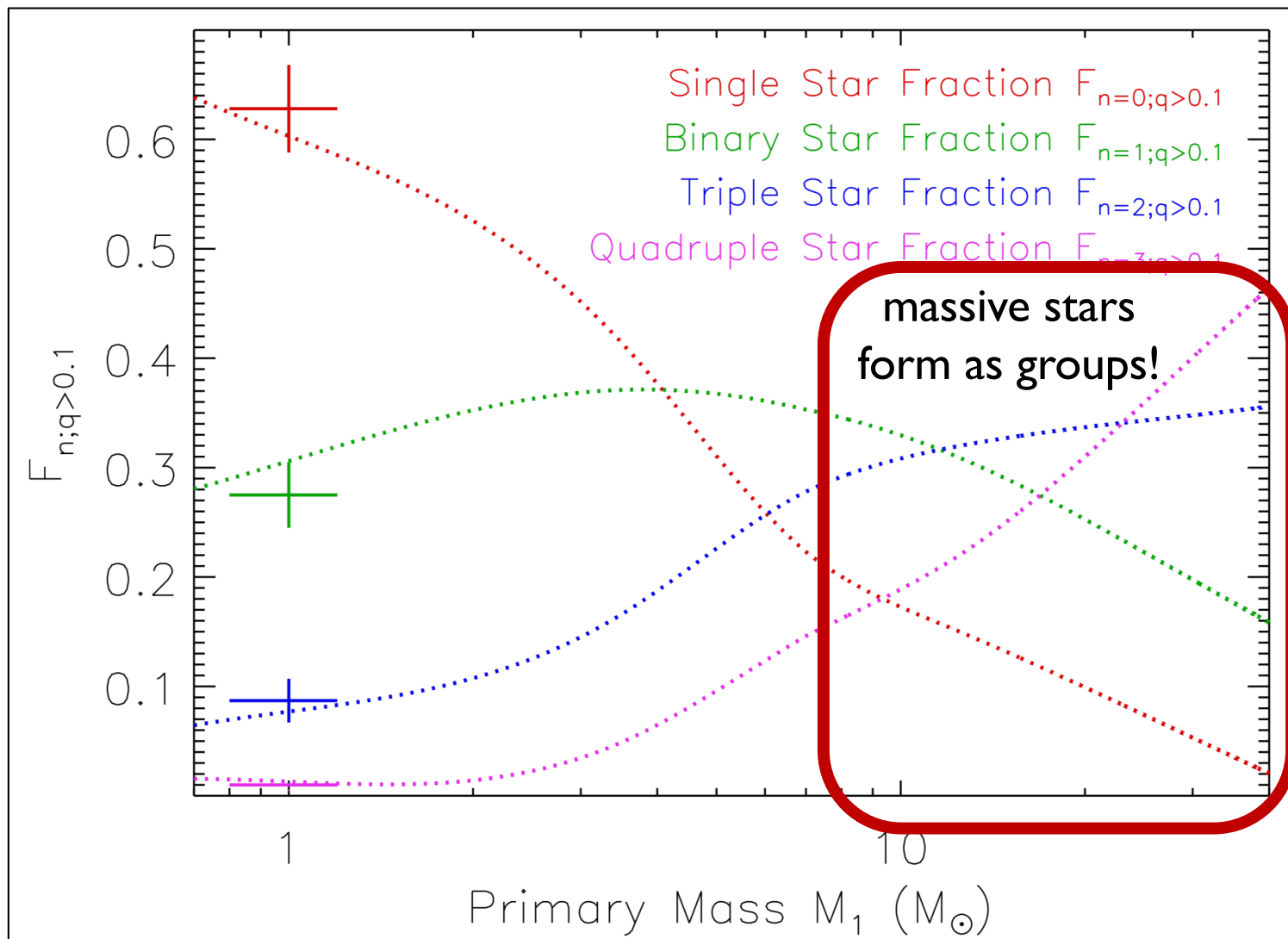
- **do the first stars also form in binaries?**



Moe et al. (2017)

- first stars – open questions

- **do the first stars also form in binaries?**



Moe et al. (2017)

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Cosmic Dawn: The First Stars & Galaxies

- the dark ages of the Universe
- the first stars
- **the first galaxies**
- implications for subsequent structure formation

- the first bound objects

- protogalaxies¹ are forming **within** dark matter halos

→ baryons fall into dark matter potential wells

¹protogalaxy = gravitationally bound gas cloud

- the first bound objects

- protogalaxies are forming **within** dark matter halos

→ baryons fall into dark matter potential wells

biased galaxy formation scenario (White & Rees 1974)

- the first bound objects – summary

- characterize DM peaks by their “height” ν

$$\nu = \frac{\delta_c}{D(a)\sigma_0(M)}, \quad \sigma_0^2(M) = \frac{1}{2\pi^2} \int_0^\infty P_0(k) \hat{W}_M^2(k) k^2 dk, \quad \ddot{D} + 2H\dot{D} - \frac{3}{2}\Omega_m H^2 D = 0$$

- compare dark matter $M_{\nu\sigma}(a)$ to its Jeans mass $M_J(a)$
- it is possible to form $3\text{-}\sigma$ dark matter haloes already at $z \approx 30$
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- the first bound objects – summary

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- the first bound objects

- number density of dark matter halos (according to Press-Schechter formalism)

$$\frac{dn}{dM} dM = \sqrt{\frac{2}{\pi}} \frac{\bar{\rho}}{M} \frac{\delta_c}{\sigma_M} \left| \frac{d \ln \sigma_M}{d \ln M} \right| \exp\left(\frac{-\delta_c^2}{2\sigma_M^2}\right) \frac{dM}{M}$$

$$\sigma_M^2 = \frac{1}{2\pi^2} \int_0^{+\infty} P(k) \hat{W}^2(kR) k^2 dk$$

$$\hat{W}(x) = \frac{3}{x^3} (\sin(x) - x \cos(x))$$

$$P(k) = \left(\frac{D(a)}{D(a_0)} \right)^2 P_0(k)$$

- the first bound objects

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combine and introduce

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- **dark matter halo mass > Jeans mass**

- ⇒ definite collapse!

- the first bound objects

!?!?!?!?

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- **dark matter halo mass** > **Jeans mass:** $M_J \propto \left(\frac{T^3}{\rho} \right)^{1/2}$

(cf. “star formation” slides)

- the first bound objects

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- the first bound objects

- **dark matter halo mass** > **Jeans mass:** $M_J \propto \left(\frac{\sigma_v^6}{\rho} \right)^{1/2}$
- $$E_{kin} = \frac{3}{2} N k_B T = \frac{1}{2} m \sigma_v^2$$

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scaling with redshift?

- the first bound objects

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$$\sigma_v \propto a^{-1}$$

$$\rho \propto a^{-3}$$

▪ the first bound objects

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\Rightarrow formation becomes easier and easier...

Note:

This Jeans mass refers to the mass of a dark matter halo, but determines whether its baryonic component is able to collapse or will be prevented from it.

- the first bound objects

• **dark matter halo mass** > **Jeans mass**: $M_J \propto \left(\frac{\sigma_v^6}{\rho} \right)^{1/2}$

evolution of $M_{\nu\sigma}(a)$?

$$\left. \begin{array}{l} \sigma_v \propto a^{-1} \\ \rho \propto a^{-3} \end{array} \right\} M_J \propto a^{-3/2} \rightarrow a \nearrow \Rightarrow M_J \searrow$$

\Rightarrow formation becomes easier and easier...

- the first bound objects

- “3- σ dark matter halos”

$$v = \frac{\delta_c}{D(z)\sigma_0(M_{3\sigma})} = 3$$

$D(z)$ = linear growth factor (cf. LSS lecture)

$$\sigma_0^2(M) = \frac{1}{2\pi^2} \int_0^\infty P_0(k) \hat{W}_M^2(k) k^2 dk$$

- the first bound objects

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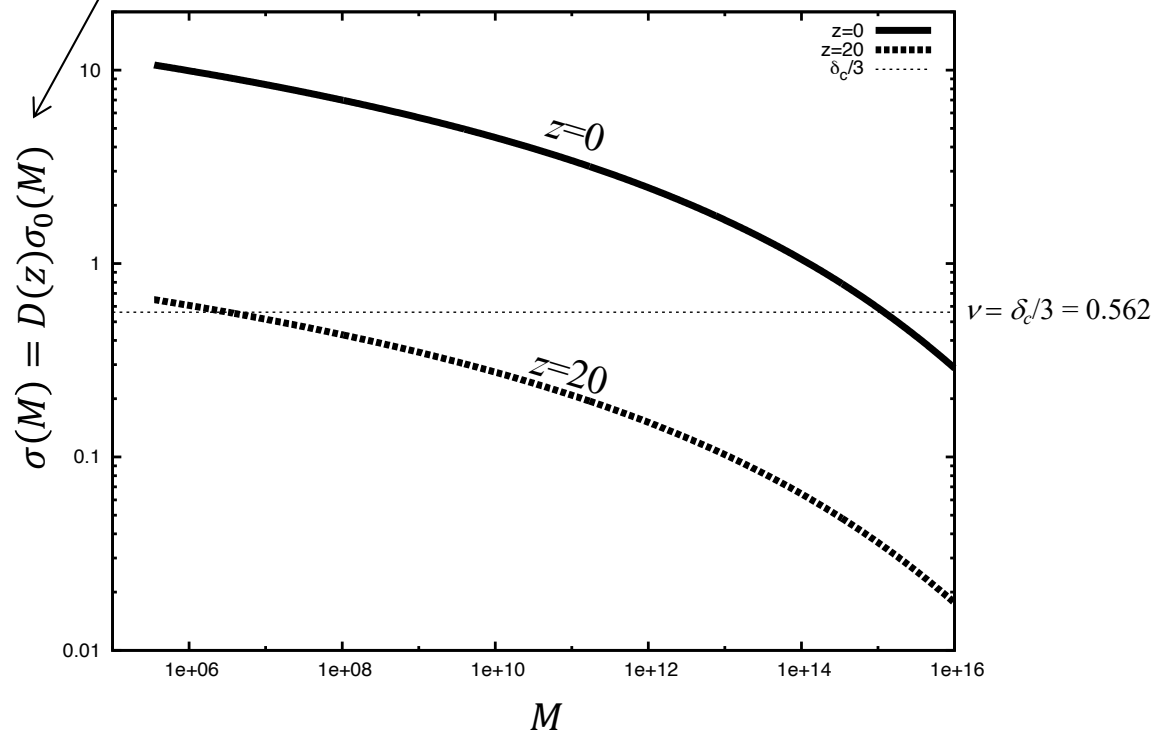
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Λ CDM model



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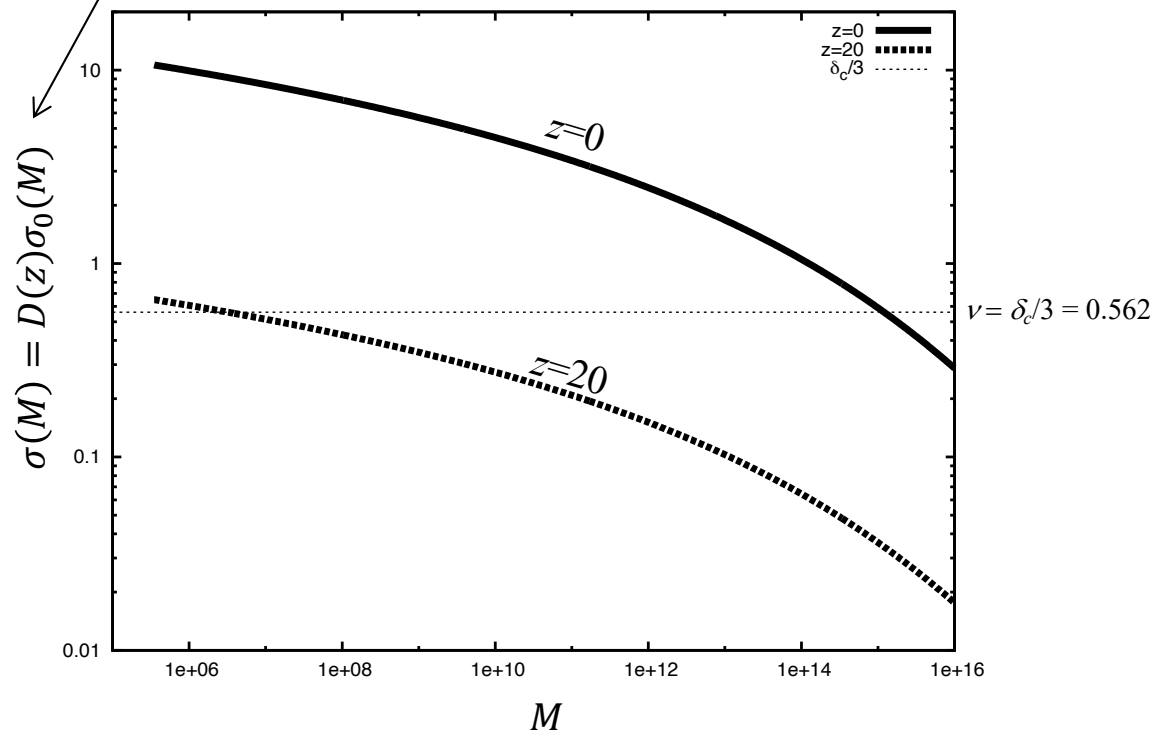
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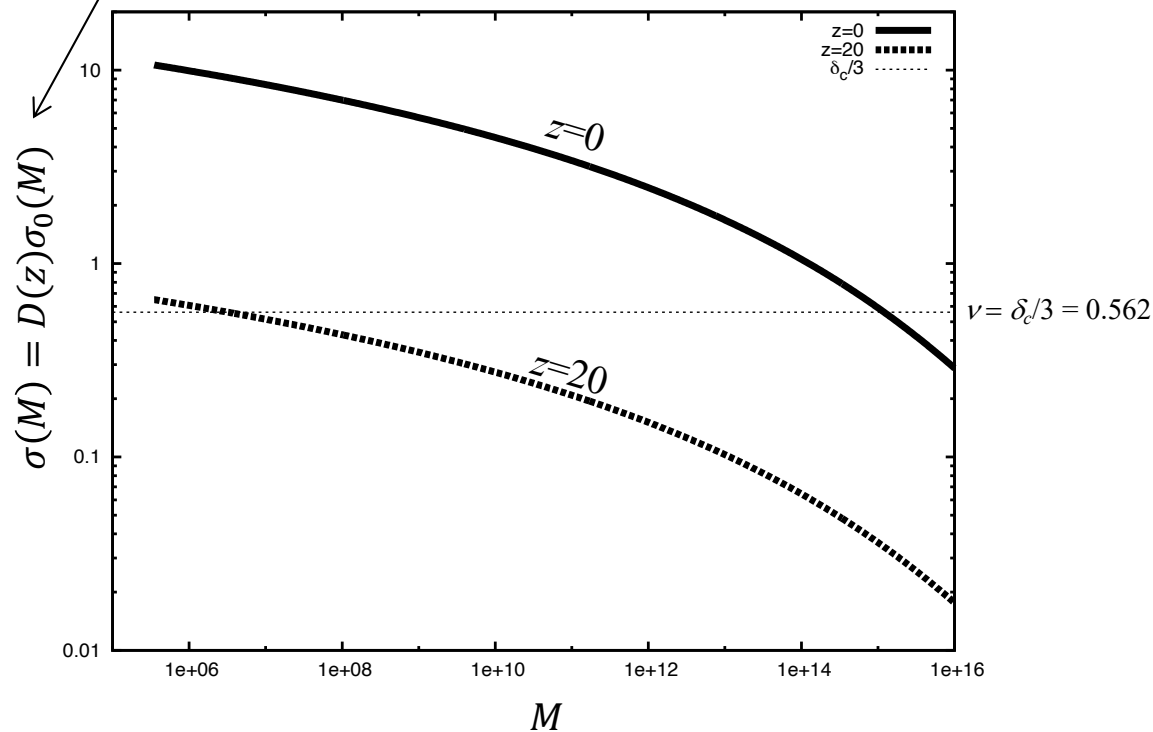
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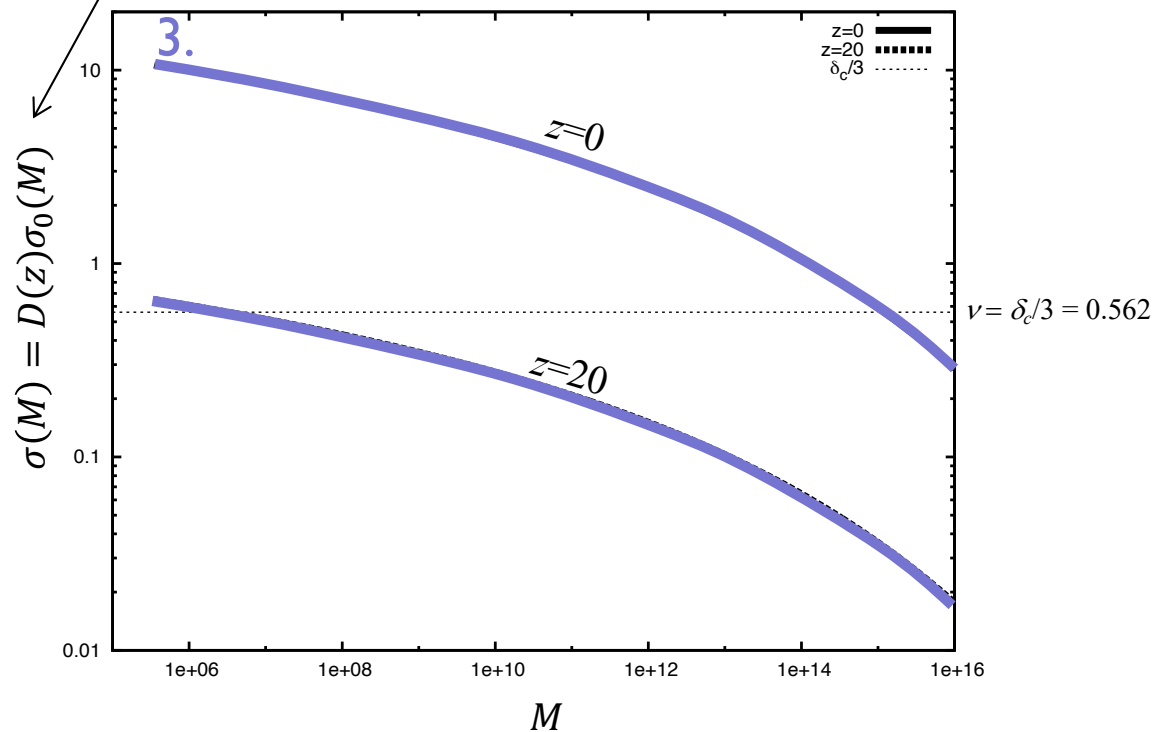
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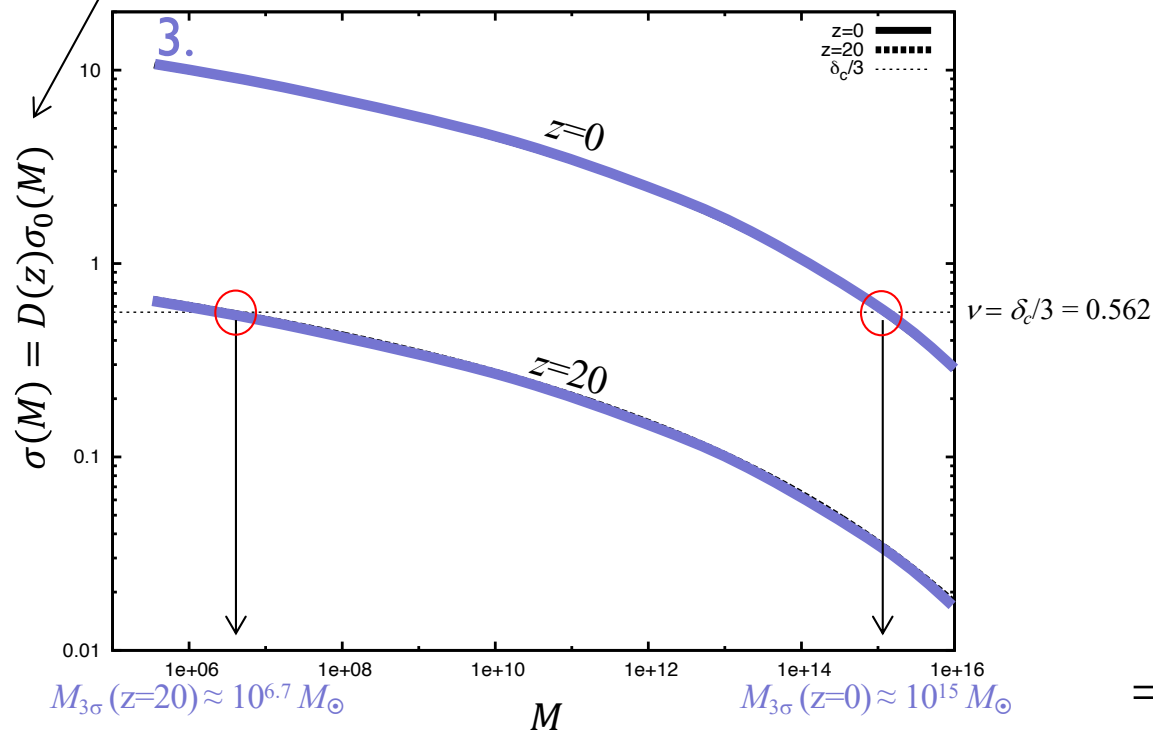
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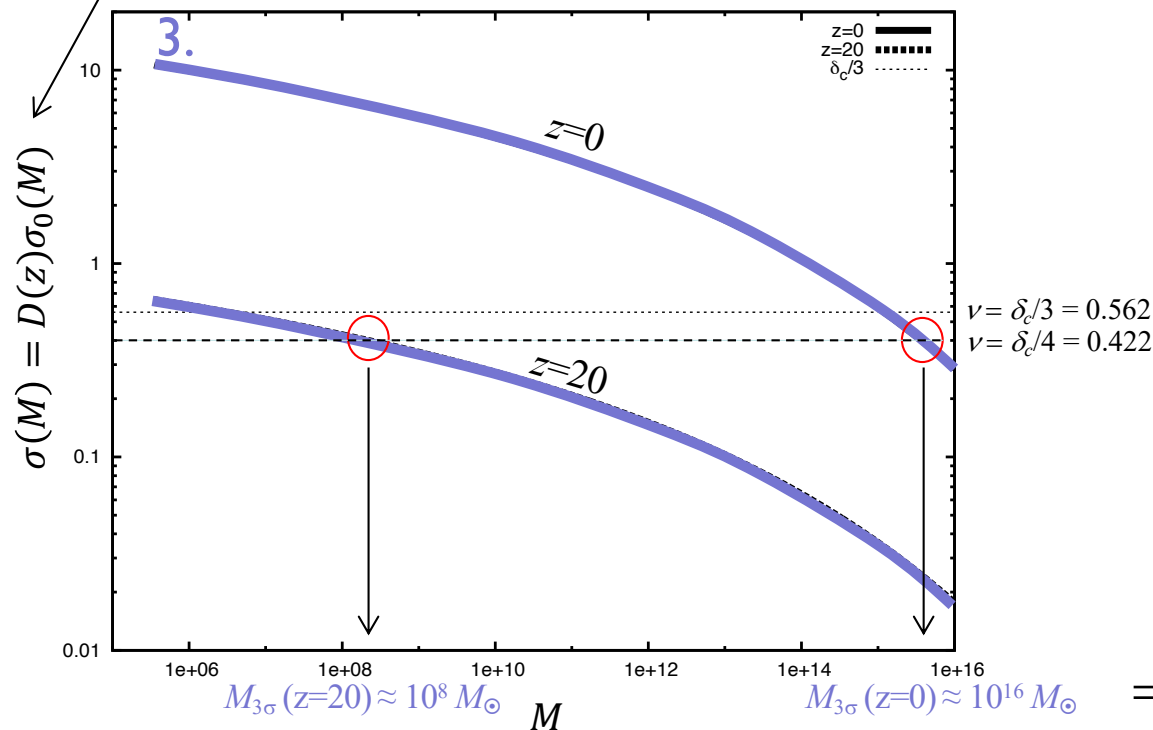
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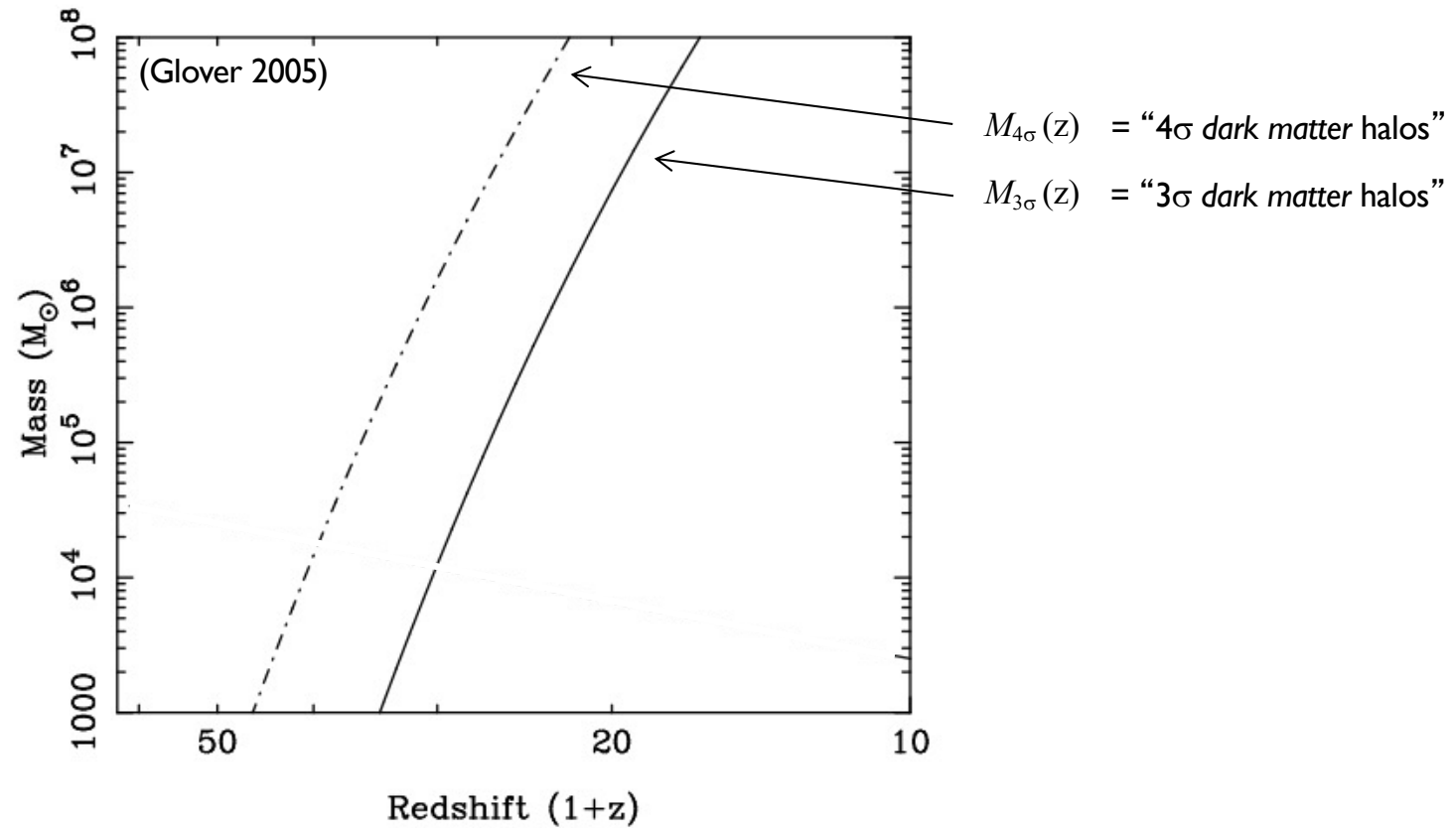
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Λ CDM model



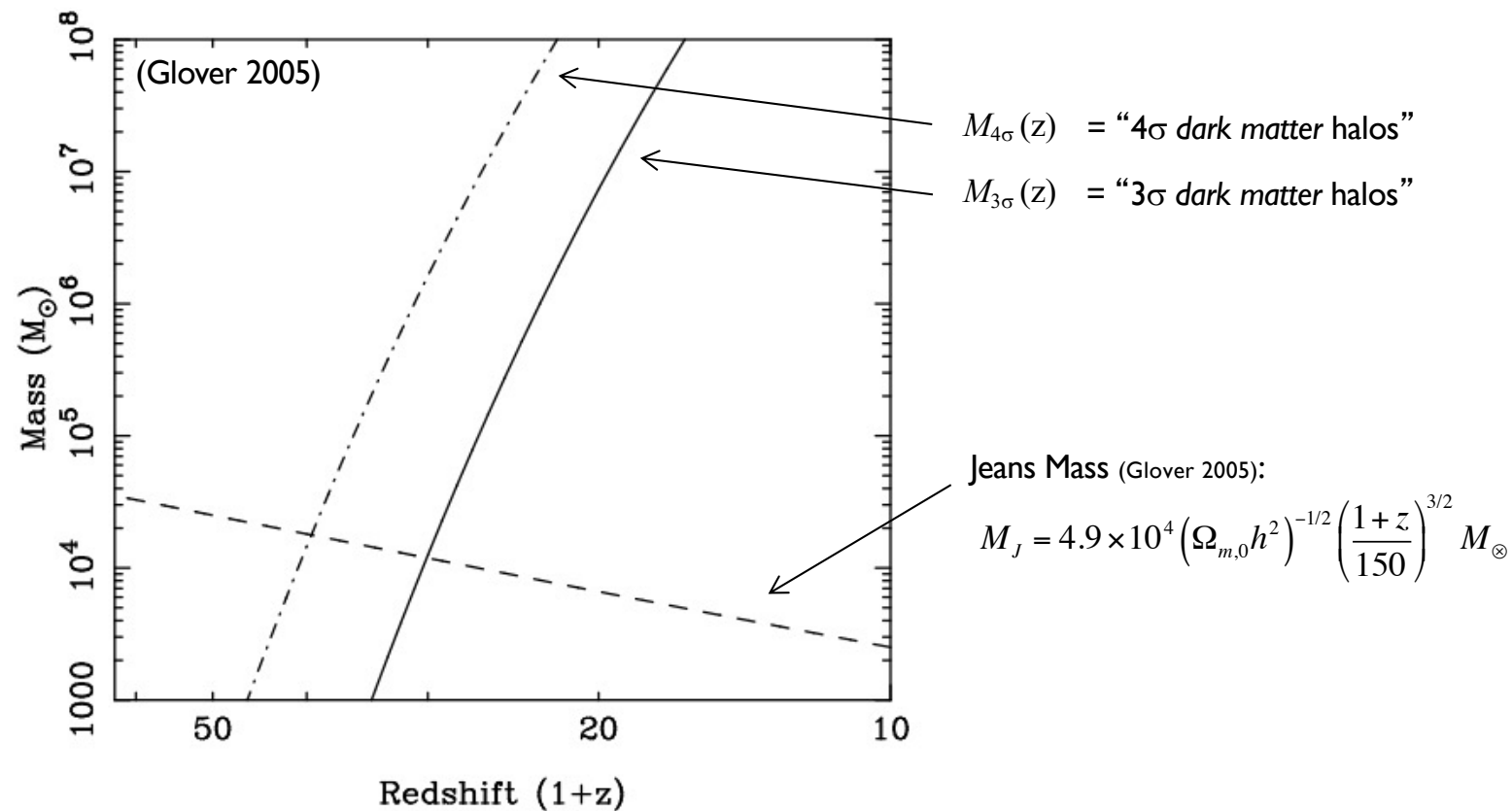
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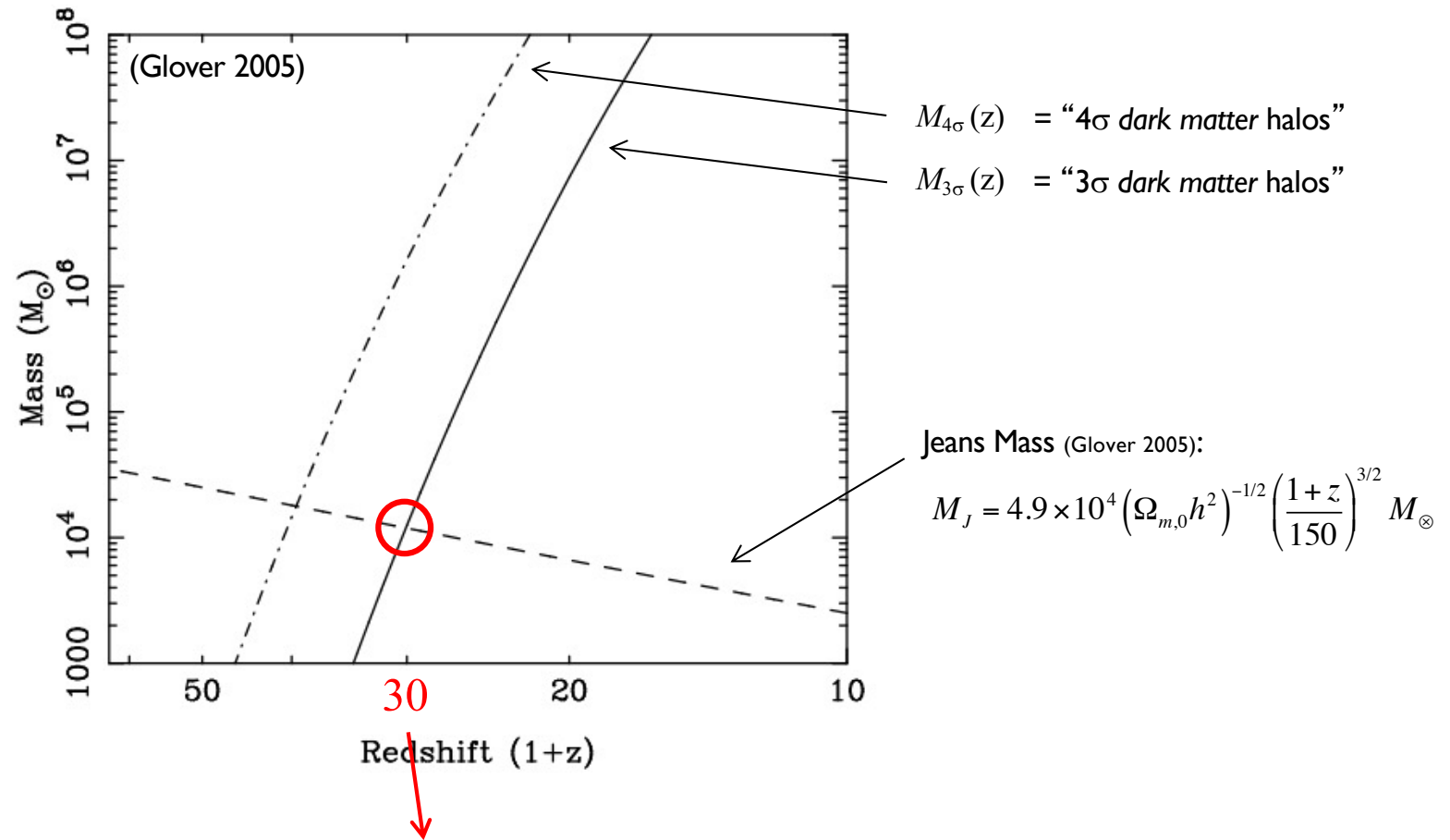
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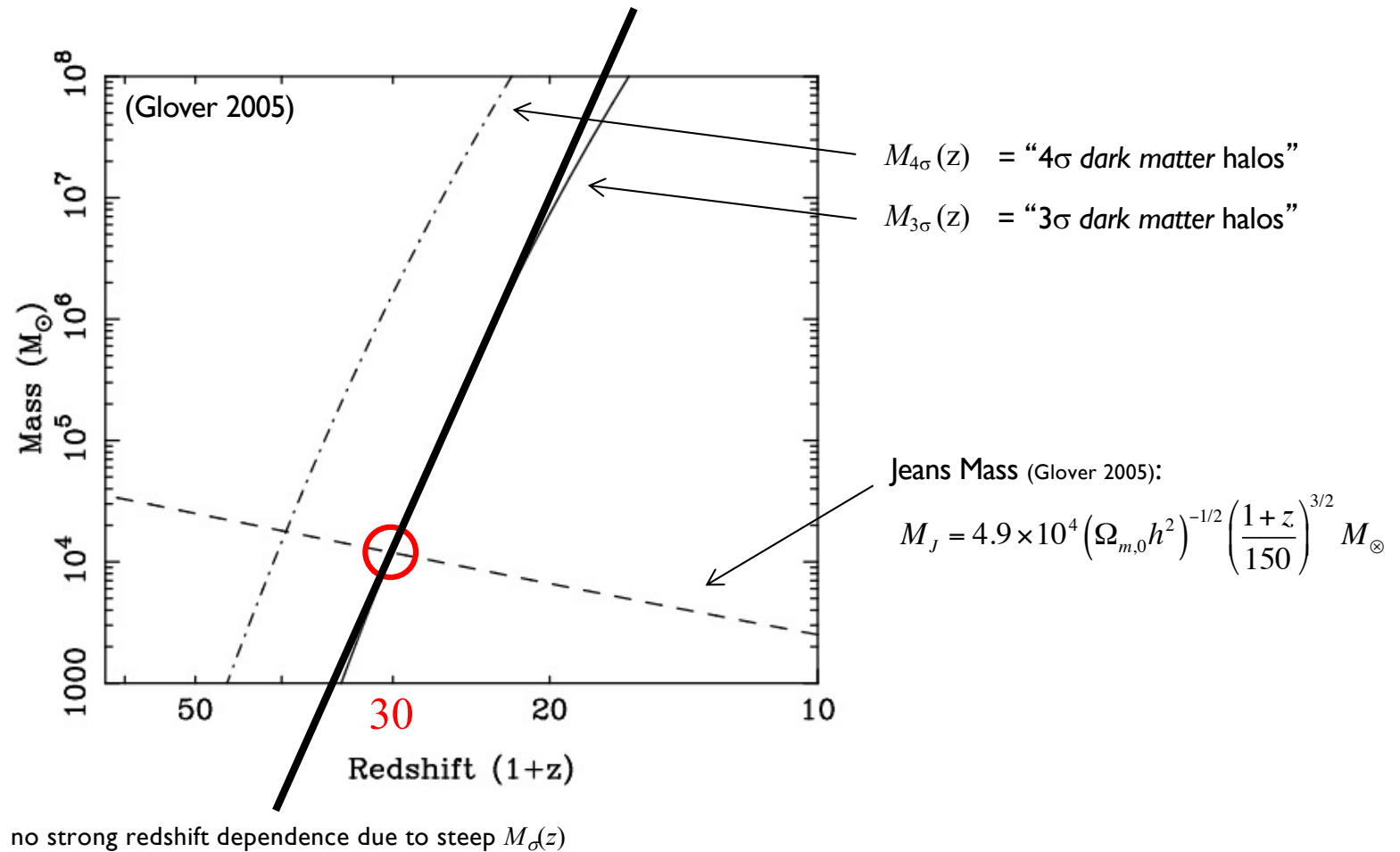
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formation of first proto-galaxies at $z \approx 30$

- the first bound objects

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▪ the first bound objects

- spherical top-hat collapse: $1 + \delta_{TH}(t_{vir}) = 18\pi^2 \approx 178$ (cf. LSS lecture)

- the first bound objects

- spherical top-hat collapse: $1 + \delta_{TH}(t_{vir}) = 18\pi^2 \approx 178$ (cf. LSS lecture)

assumption of virial theorem in derivation!

...but how do dark matter haloes reach it?

- the first bound objects

- spherical top-hat collapse: $1 + \delta_{TH}(t_{vir}) = 18\pi^2 \approx 178$ (cf. LSS lecture)
- relaxation & virialisation:
 - *relaxation*: process by which system acquires equilibrium*
 - *virialisation*: finally reaching virial equilibrium $2T = -U$

*re-distribute gravitational collapse energy into random motion

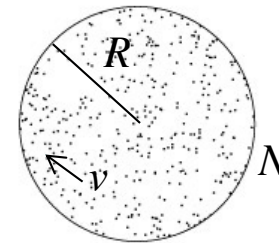
- the first bound objects

- spherical top-hat collapse: $1 + \delta_{TH}(t_{vir}) = 18\pi^2 \approx 178$ (cf. LSS lecture)
- relaxation towards virial equilibrium:
 - *two-body relaxation*: two-body interactions
 - *violent relaxation*: change in energy due to change in overall potential
 - *phase-mixing*: spreading of phase-space due to different frequencies of orbits
 - *chaotic mixing*: spreading of phase-space due to chaotic nature of orbits
 - *Landau damping*: damping and decay of perturbations

- the first bound objects

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- relaxation towards virial equilibrium:
 - *two-body relaxation*: two-body interactions

$$t_{relax} \approx \frac{N}{10 \ln N} t_{cross}, \quad t_{cross} \approx \frac{R}{v}$$



$$t_{relax} \gg t_{Hubble}$$

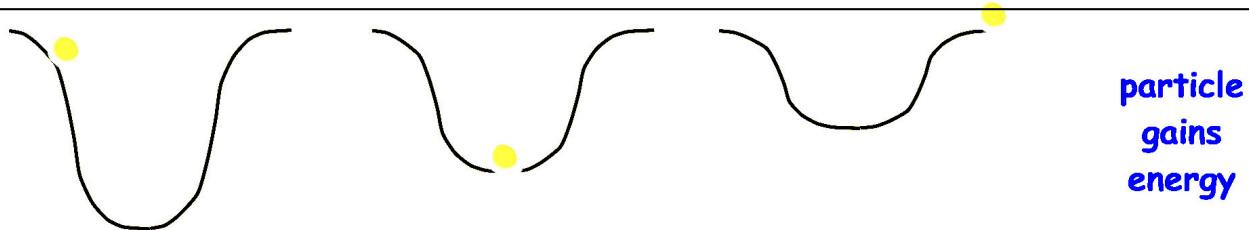
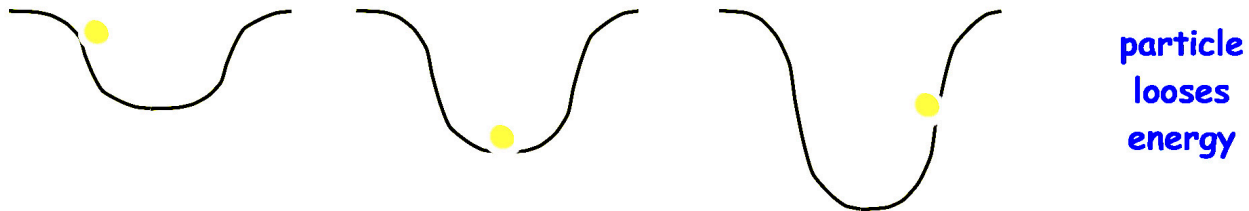
(for all cosmological objects of interest to us...)

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remember:
our objects are collapsing



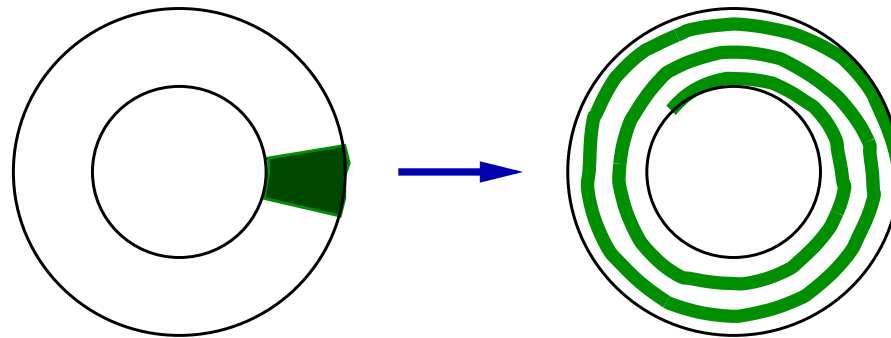
time

- the first bound objects

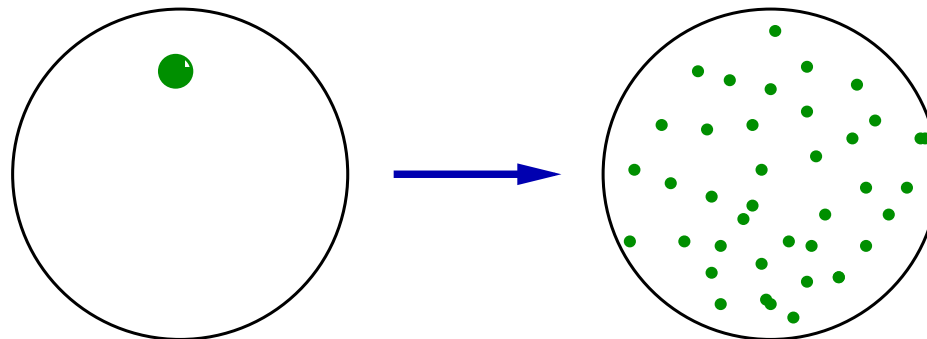
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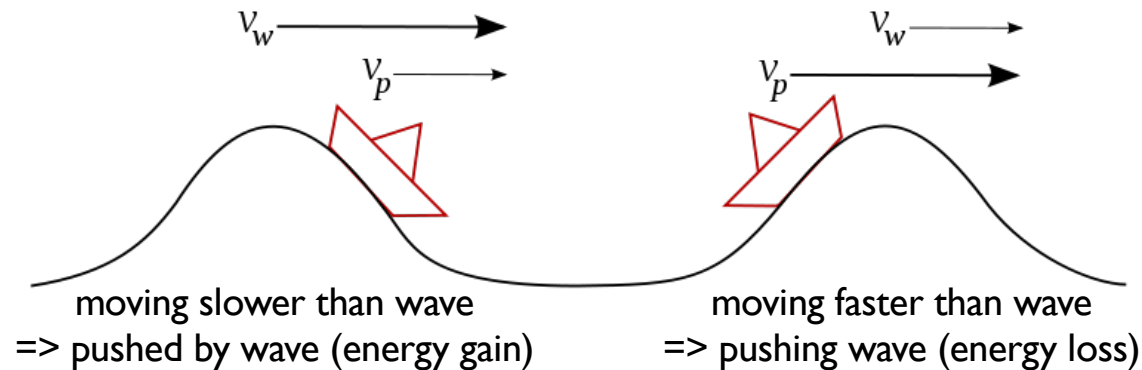


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- the first bound objects

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- relaxation towards virial equilibrium:
 - *Landau damping*: damping and decay of perturbations...
...due to interaction of particles with (density) waves



- the first bound objects – summary

- characterize DM peaks by their “height” ν

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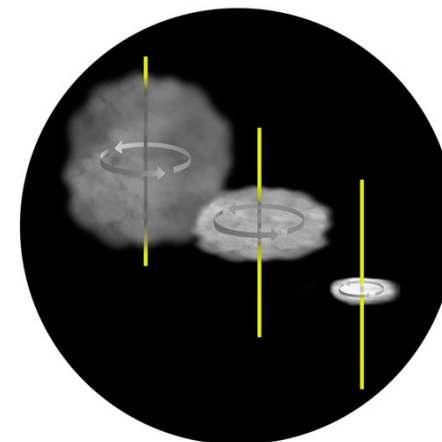
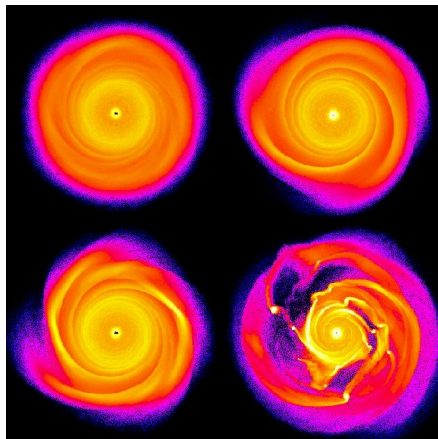
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...and what about the proto-galaxies now?

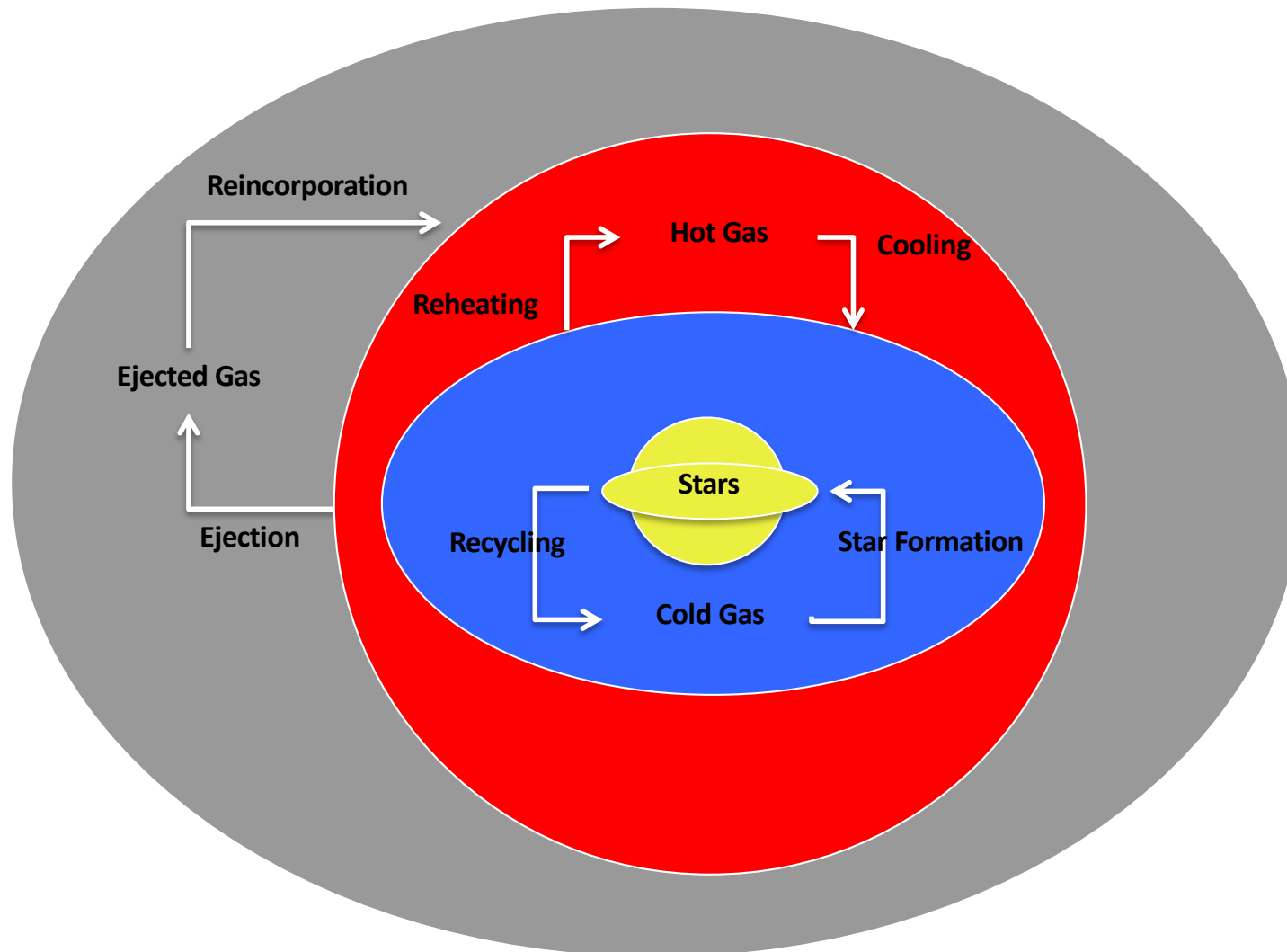
▪ proto-galaxies

- presence of DM halo appears inevitable, but
- potential well of DM halo needs to be sufficiently deep to retain gas heated to high temperatures ($>10^4\text{K}$) by first stars
- cooling of gas cloud required
- collapse to disk-like structure because of angular momentum* conservation
- fragmentation via turbulence

*tidal torque theory: anisotropic collapse of δ

- proto-galaxies

- complexity of galaxy formation in general:



Cosmic Dawn: The First Stars & Galaxies

- the dark ages of the Universe
- the first stars
- the first galaxies
- **implications for subsequent structure formation**

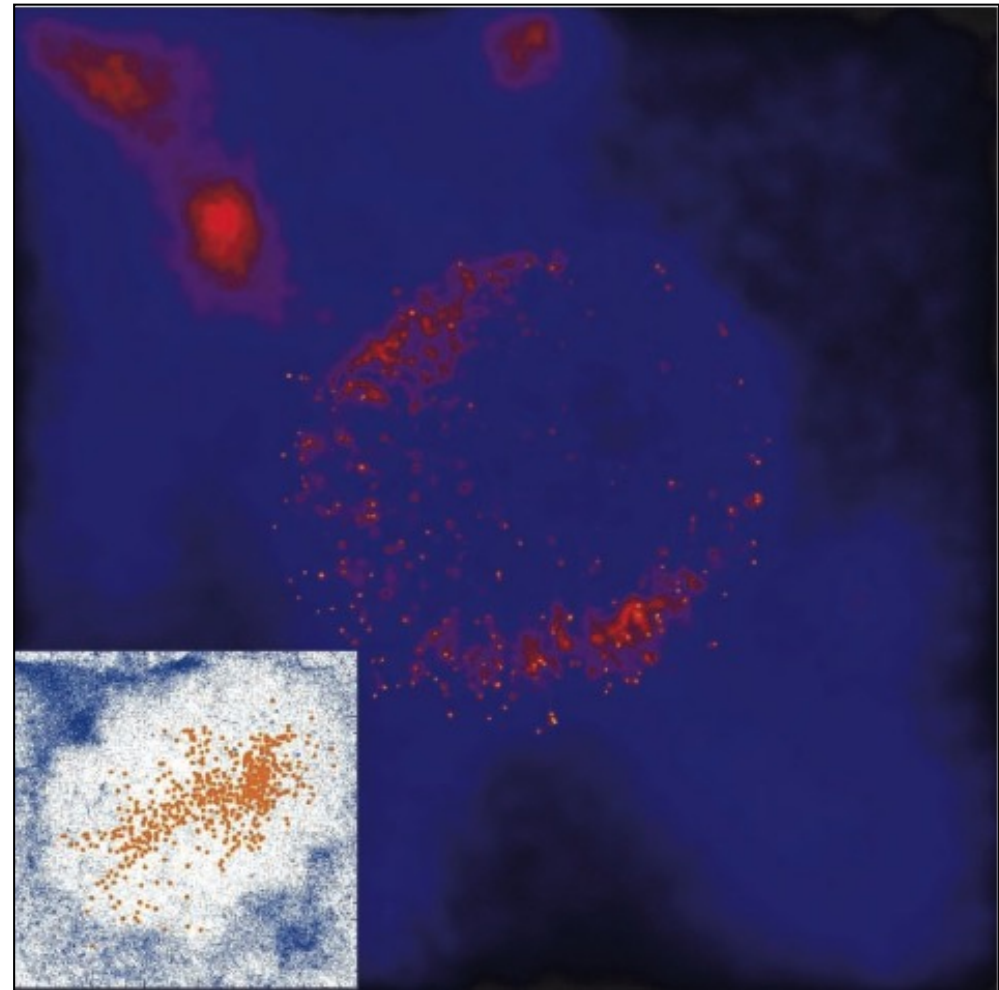
▪ proto-galaxies

- enrichment of the Universe with heavy elements
- re-ionisation of the Universe

→ first objects affect everything that comes afterwards

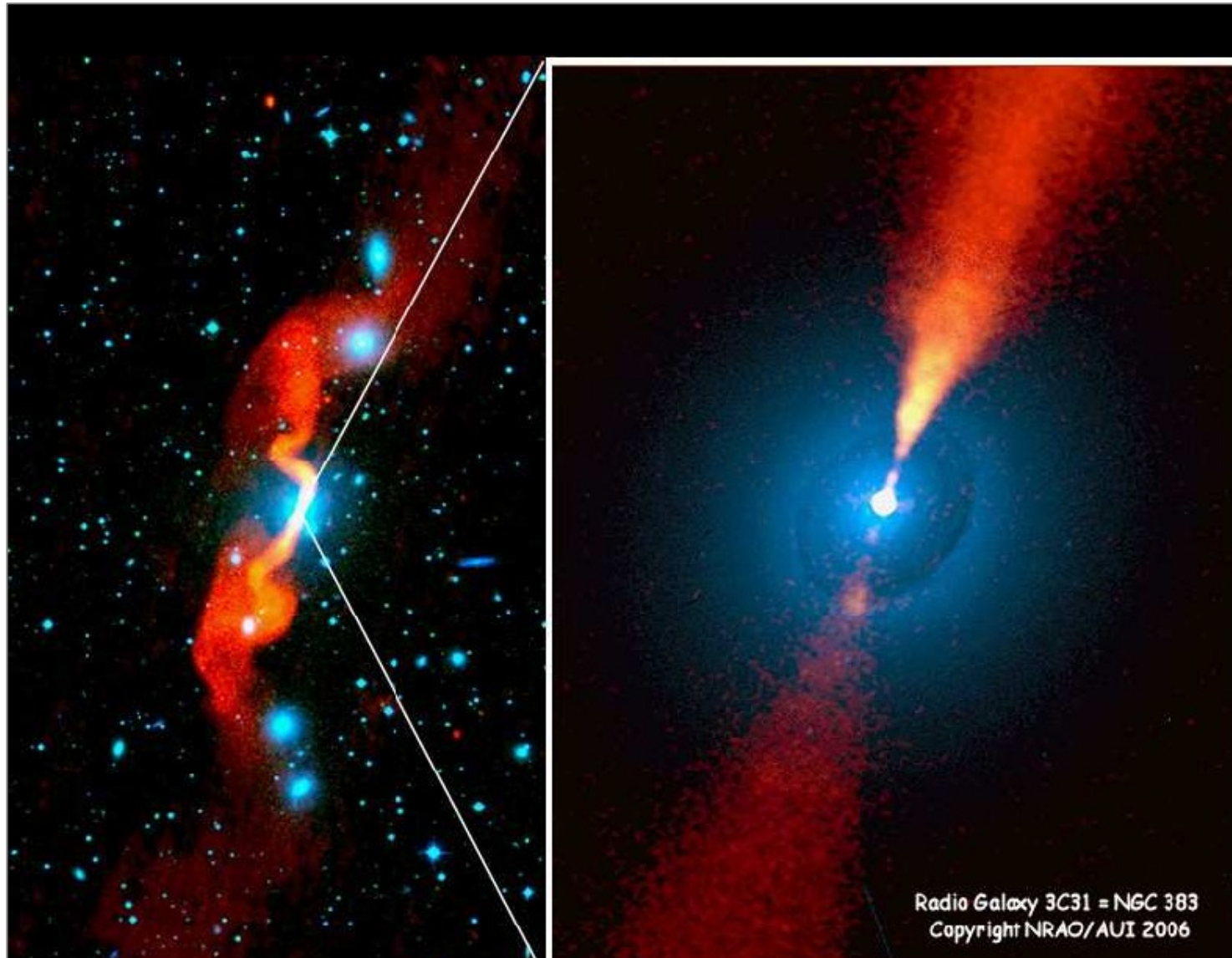
- the first supernova explosion

- explosion after ca. 10^6 years
- $E_{\text{SN}} = 10^{53}$ ergs
- color-coded gas density after 1 Myr
 - red dots = stellar ejecta
 - blue dots = HII regions
- inset panel:
 - metal distribution after 3 Myrs

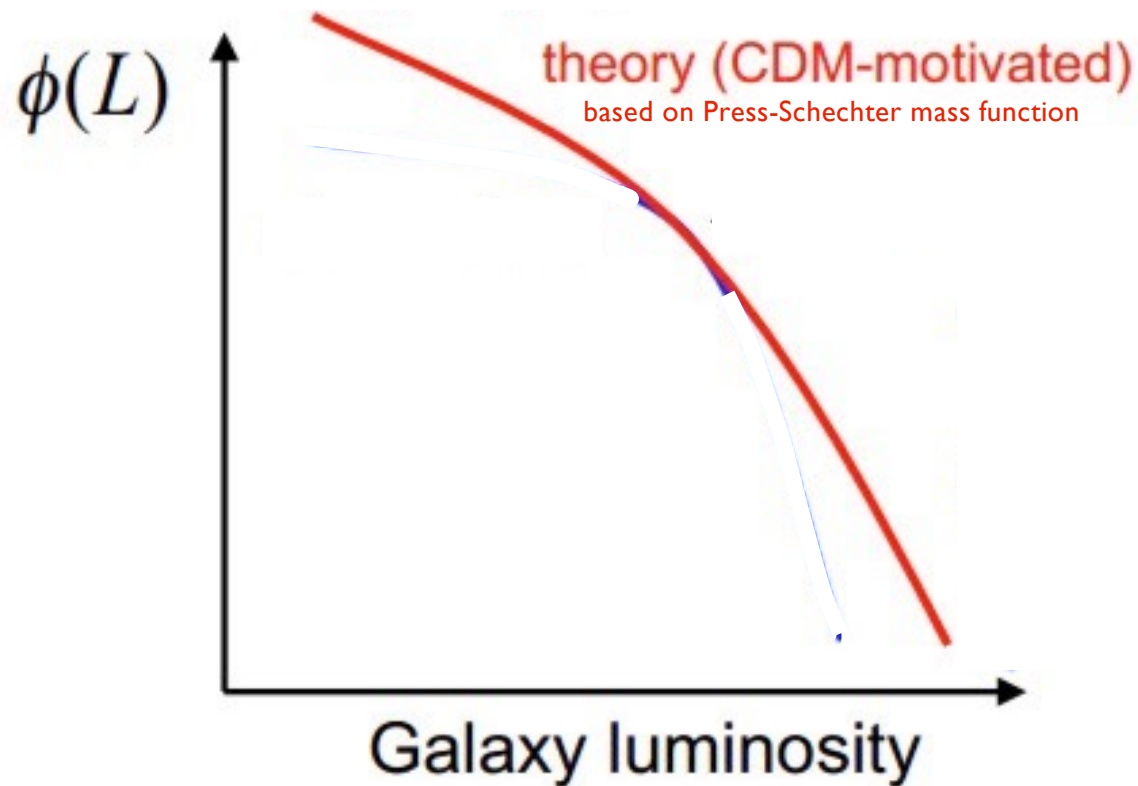


1 kpc

▪ Active Galactic Nuclei

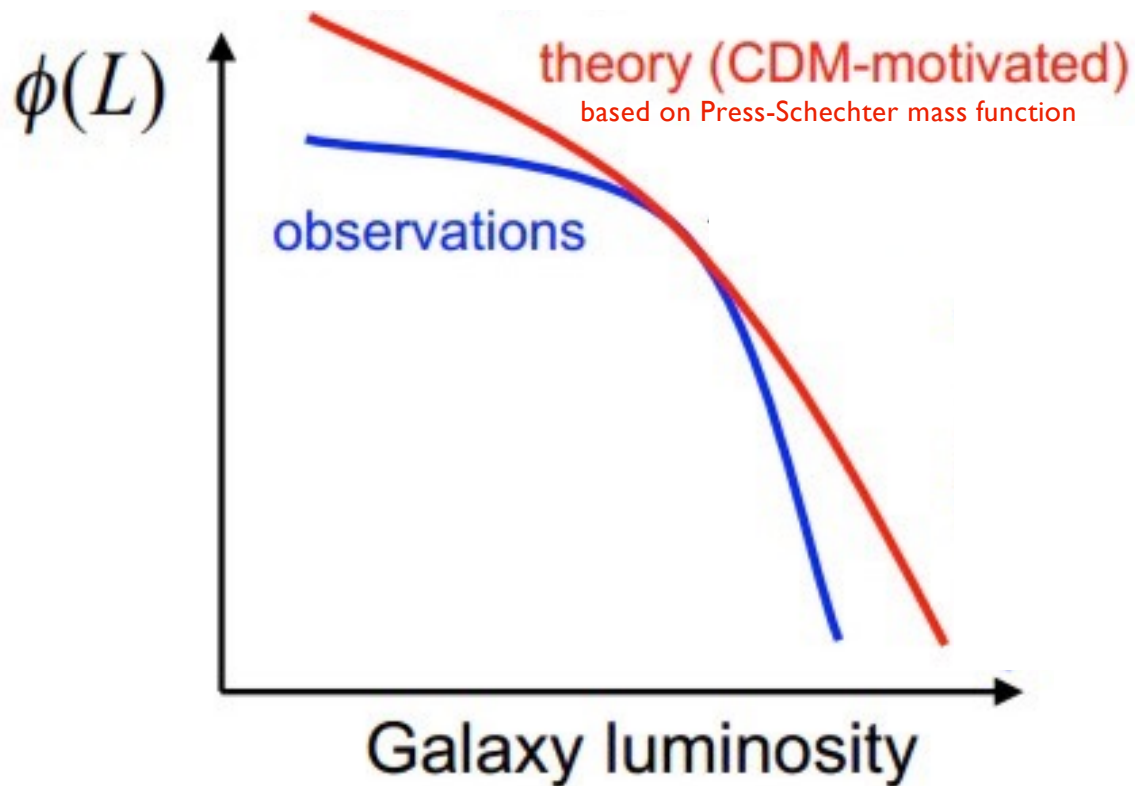


- shaping the luminosity function of galaxies



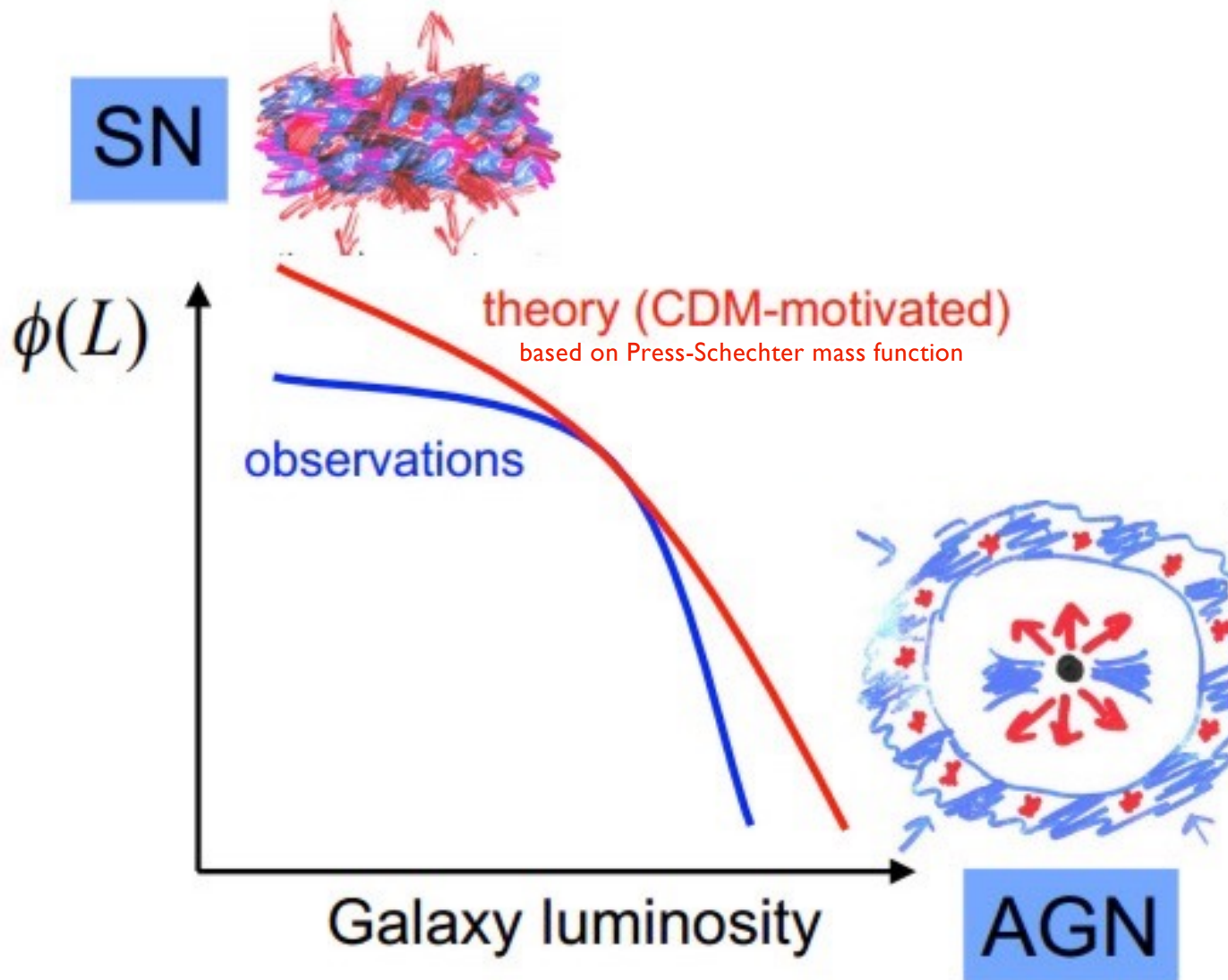
(Silk et al., 2013)

- shaping the luminosity function of galaxies



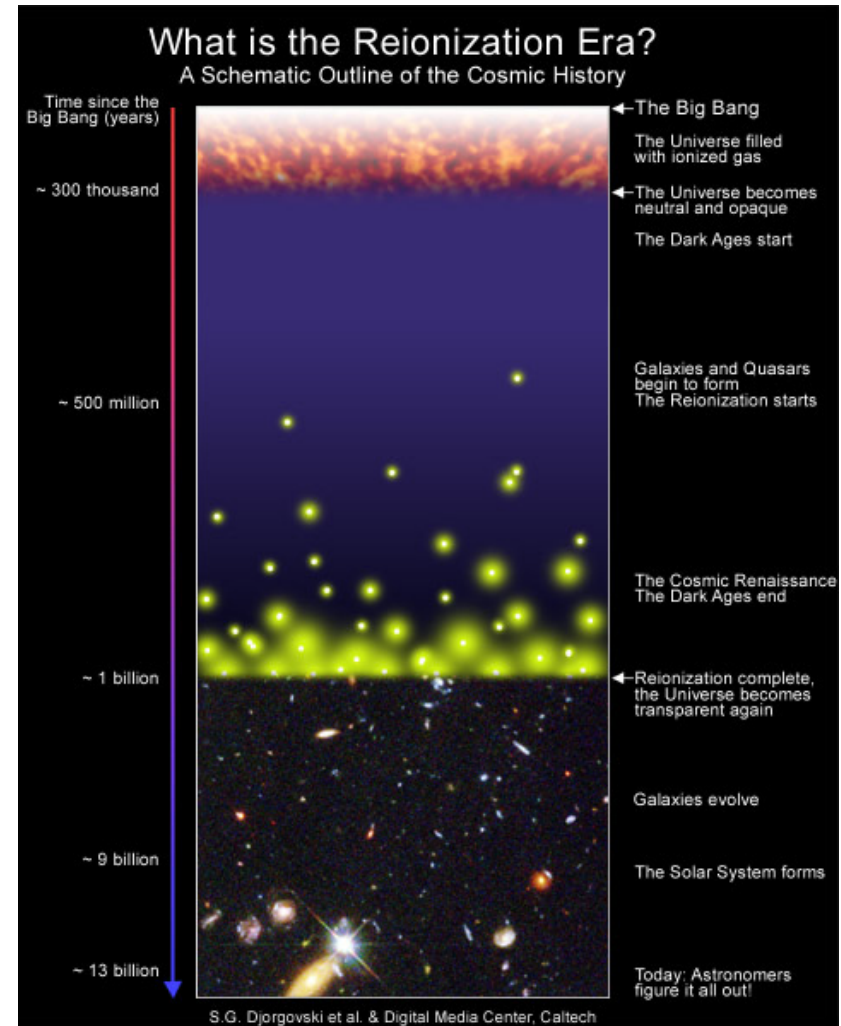
(Silk et al., 2013)

- shaping the luminosity function of galaxies



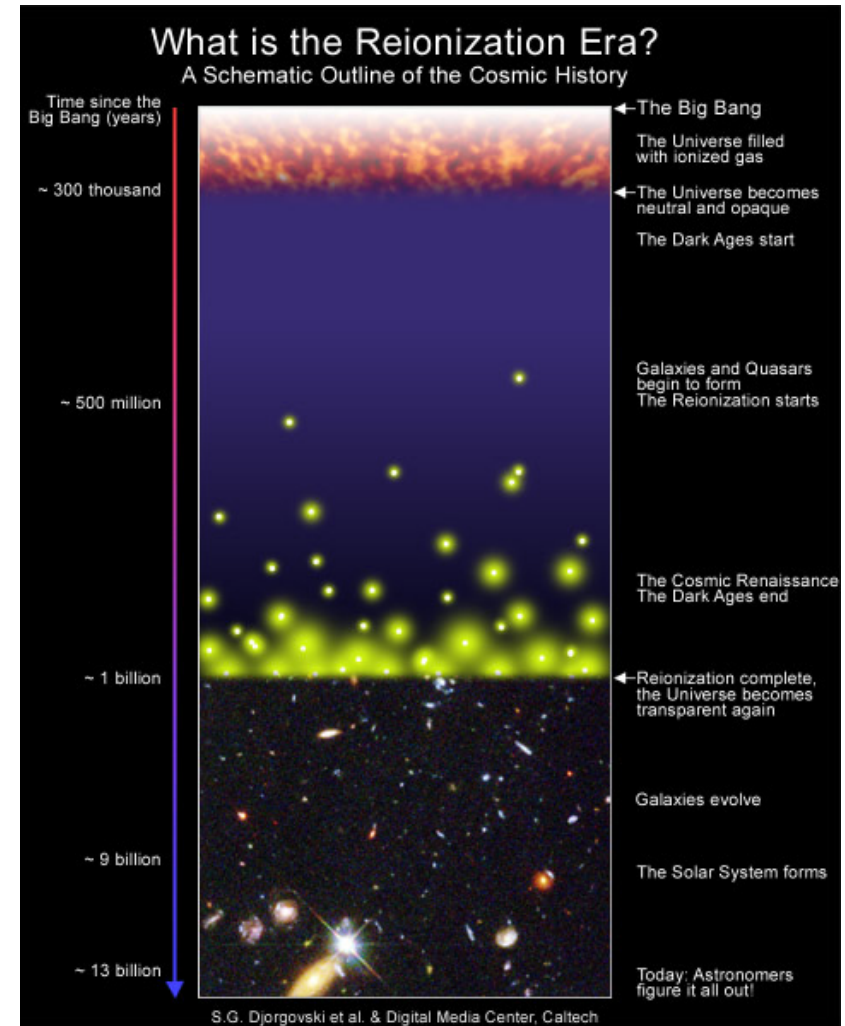
(Silk et al., 2013)

■ reionising the Universe



■ reionising the Universe

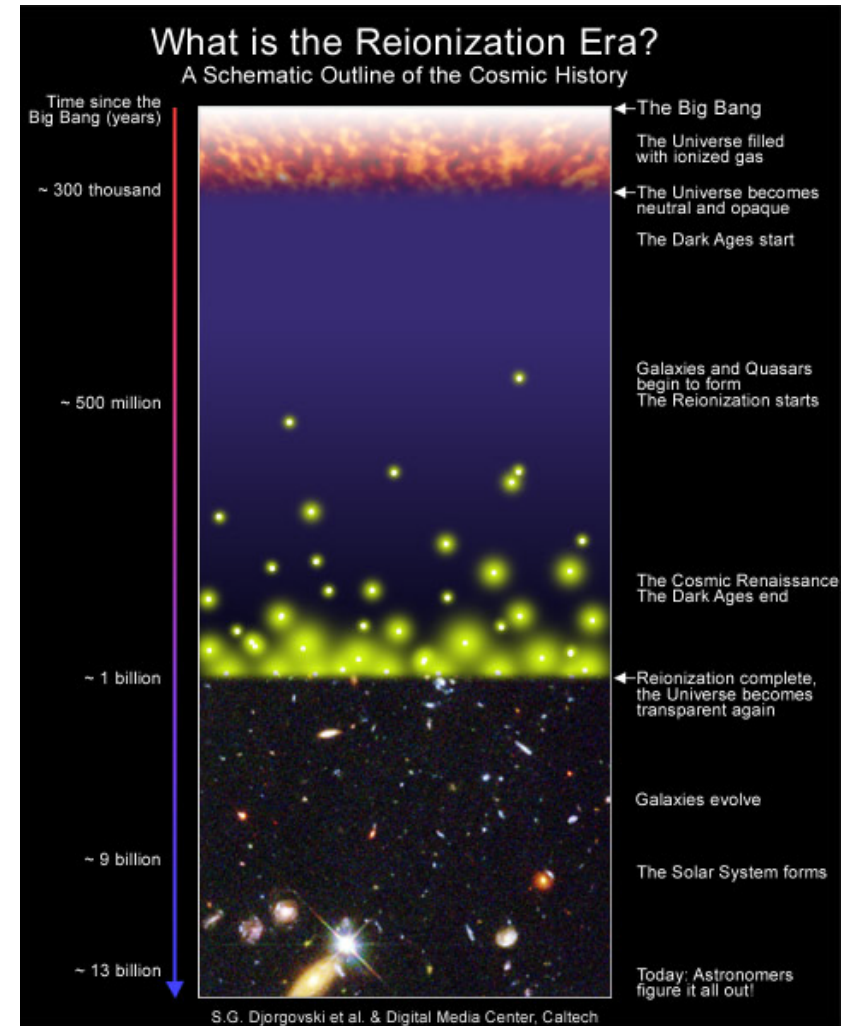
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- detected via...
 - ...Gunn-Peterson trough in QSO spectra:
neutral hydrogen along line-of-sight absorbs photons



▪ reionising the Universe

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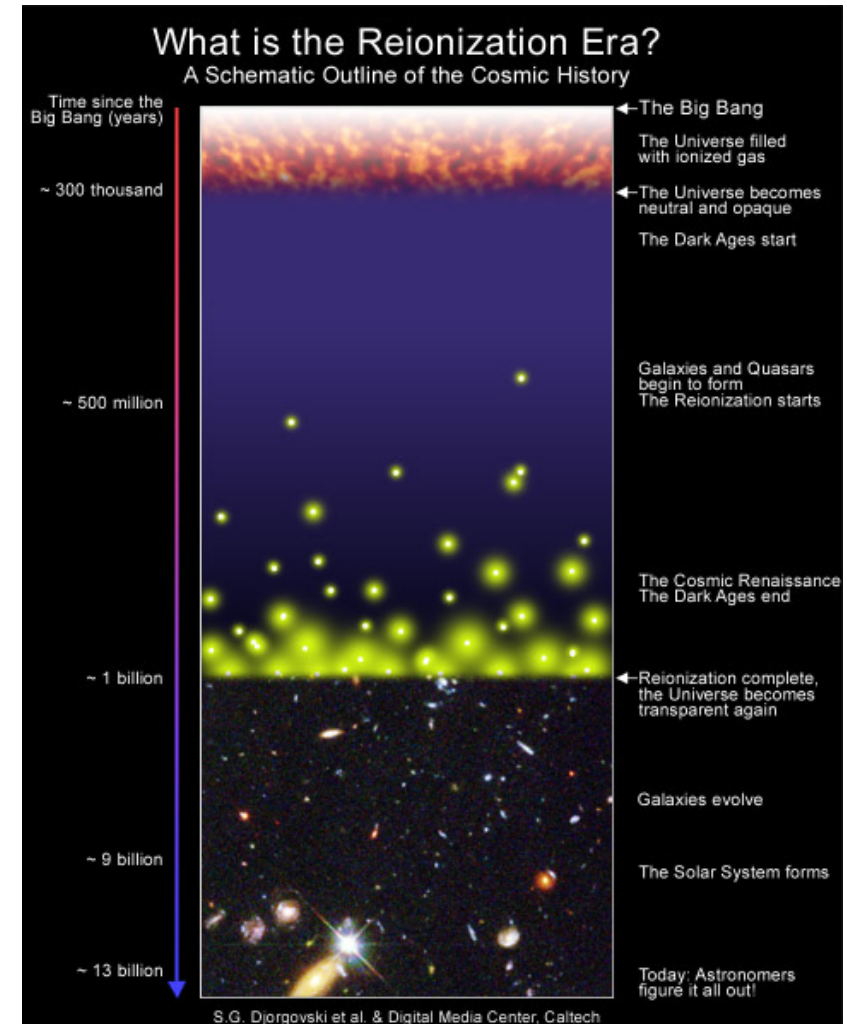


■ reionising the Universe

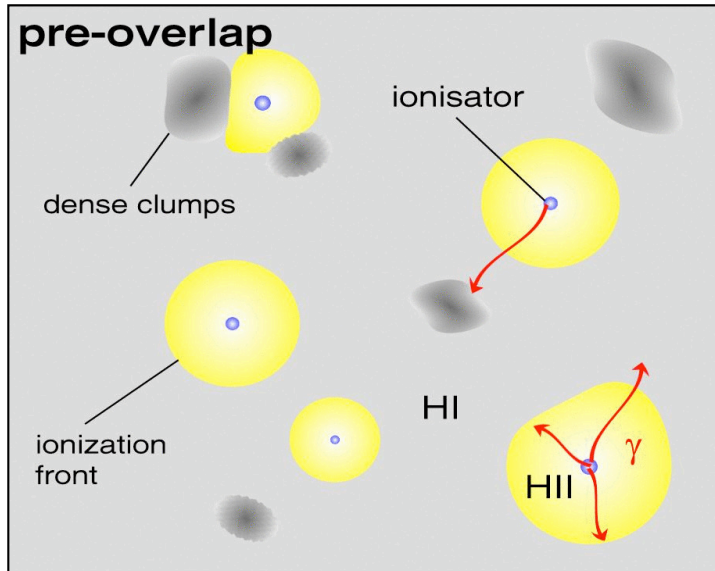
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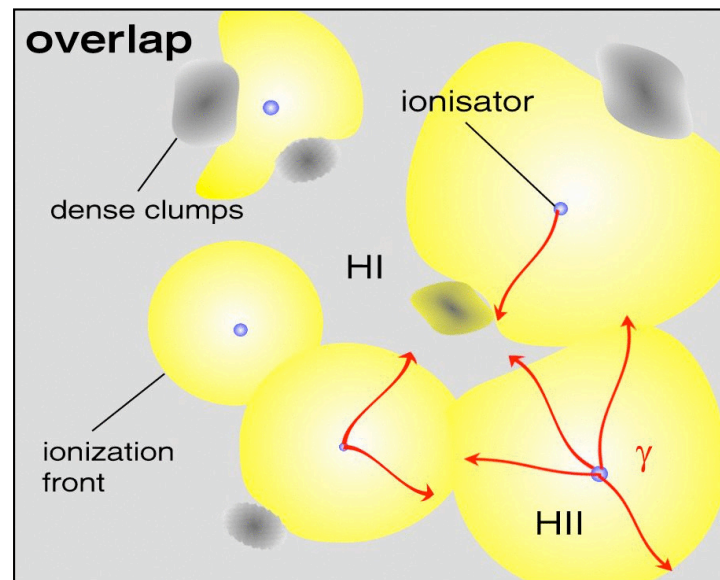
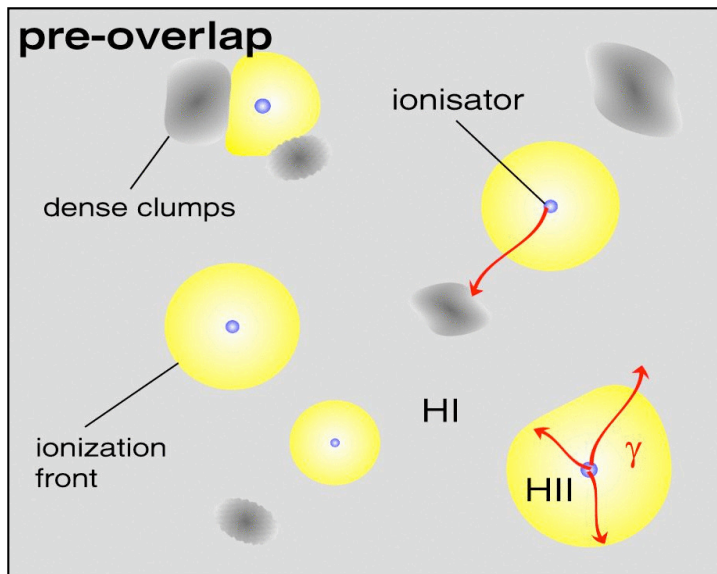
...Thomson scattering of CMB photons:
erasing of small scale anisotropies, polarization of CMB,
Planck 2013: reionisation started at $z \approx 11$



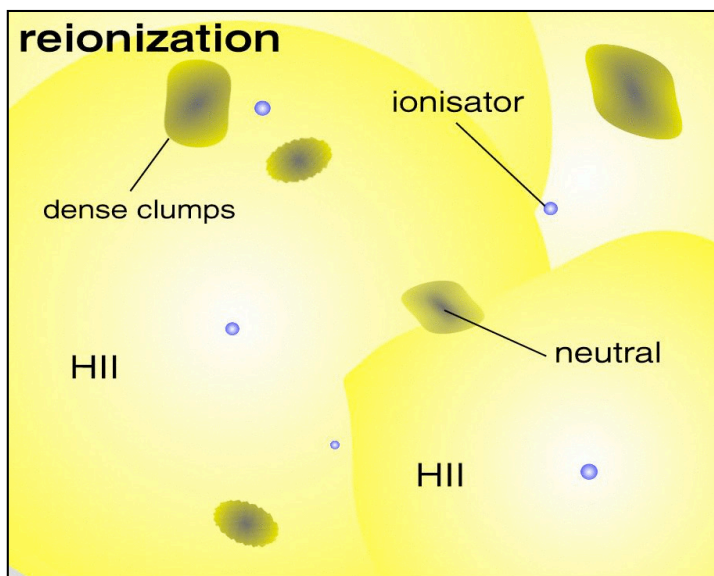
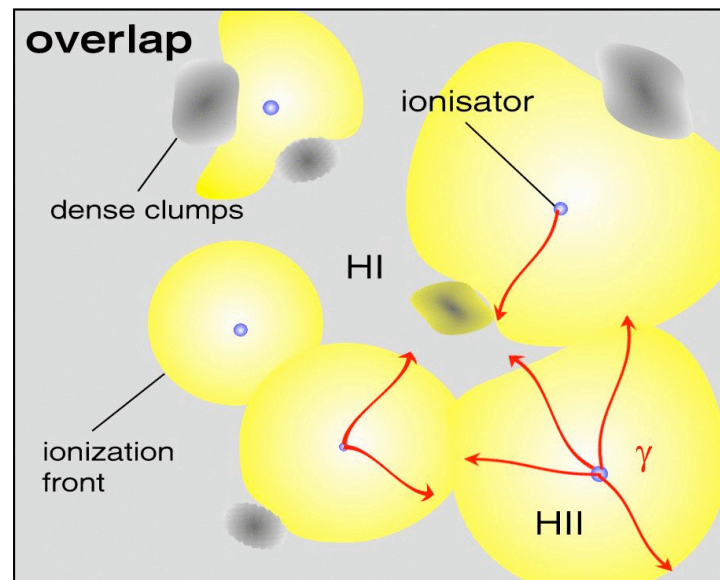
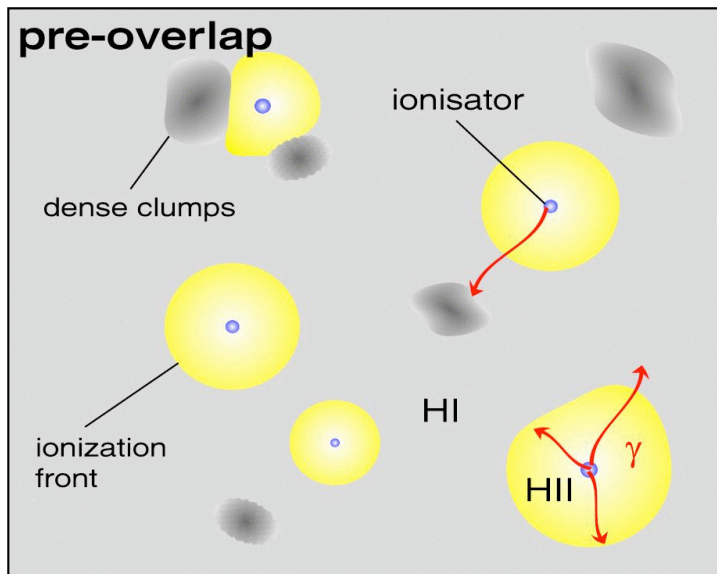
■ reionising the Universe - inhomogeneous process



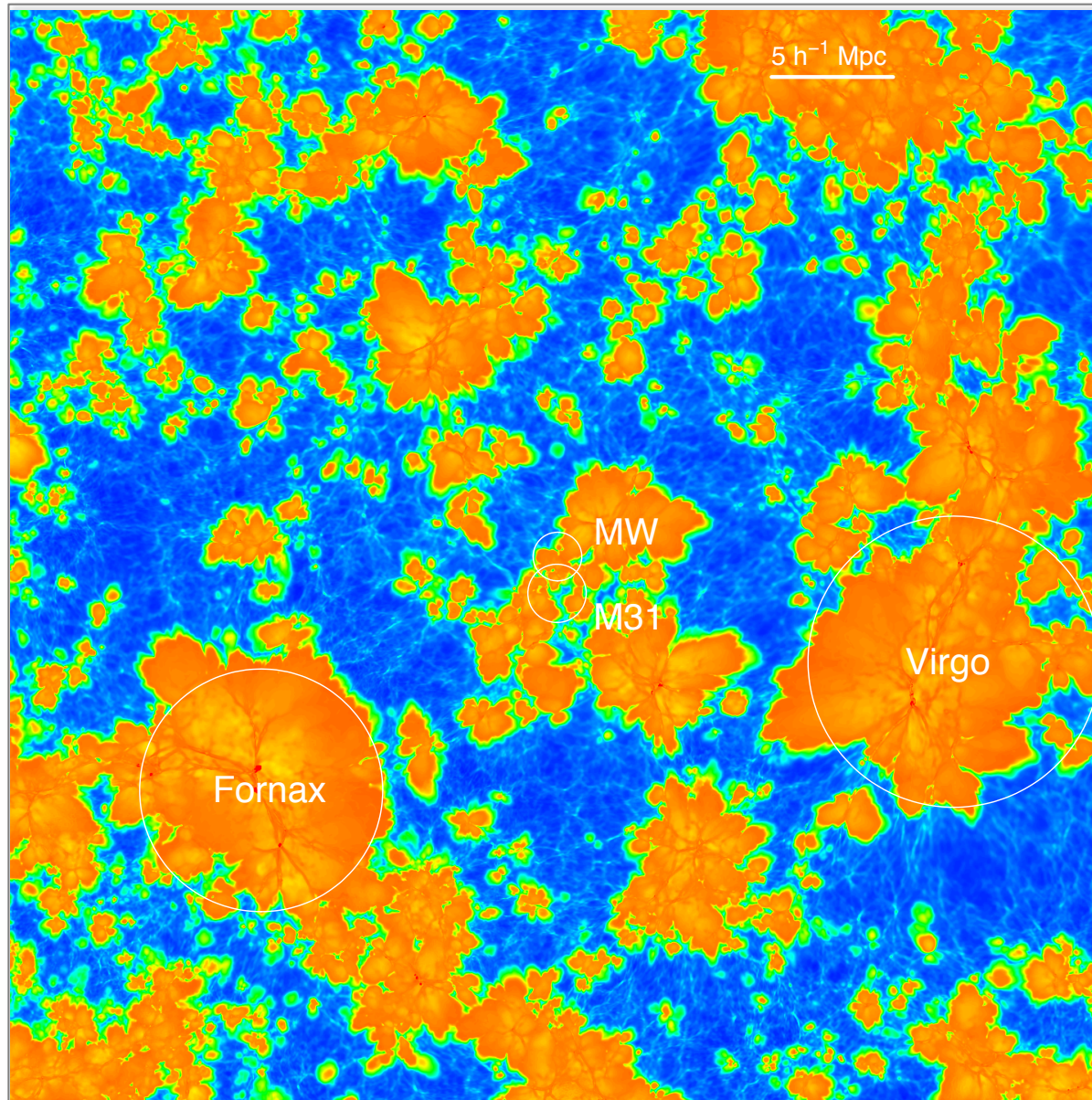
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■ reionising the Universe - inhomogeneous process

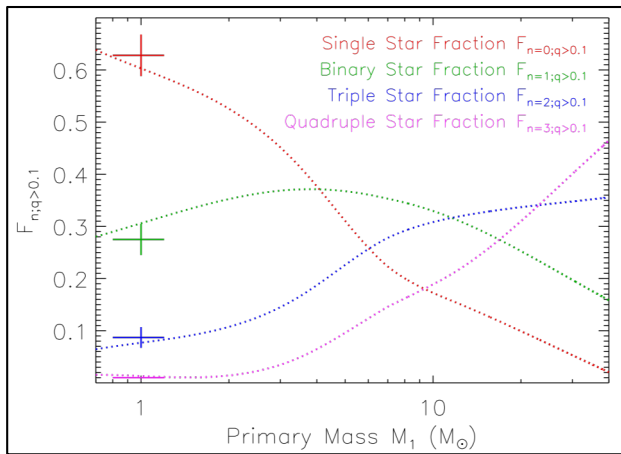
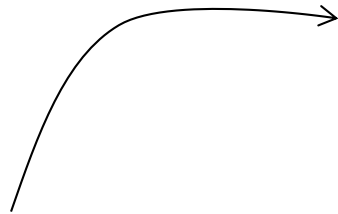


- reionising the Universe - Cosmic Dawn simulation (Ocvirk et al. 2016)



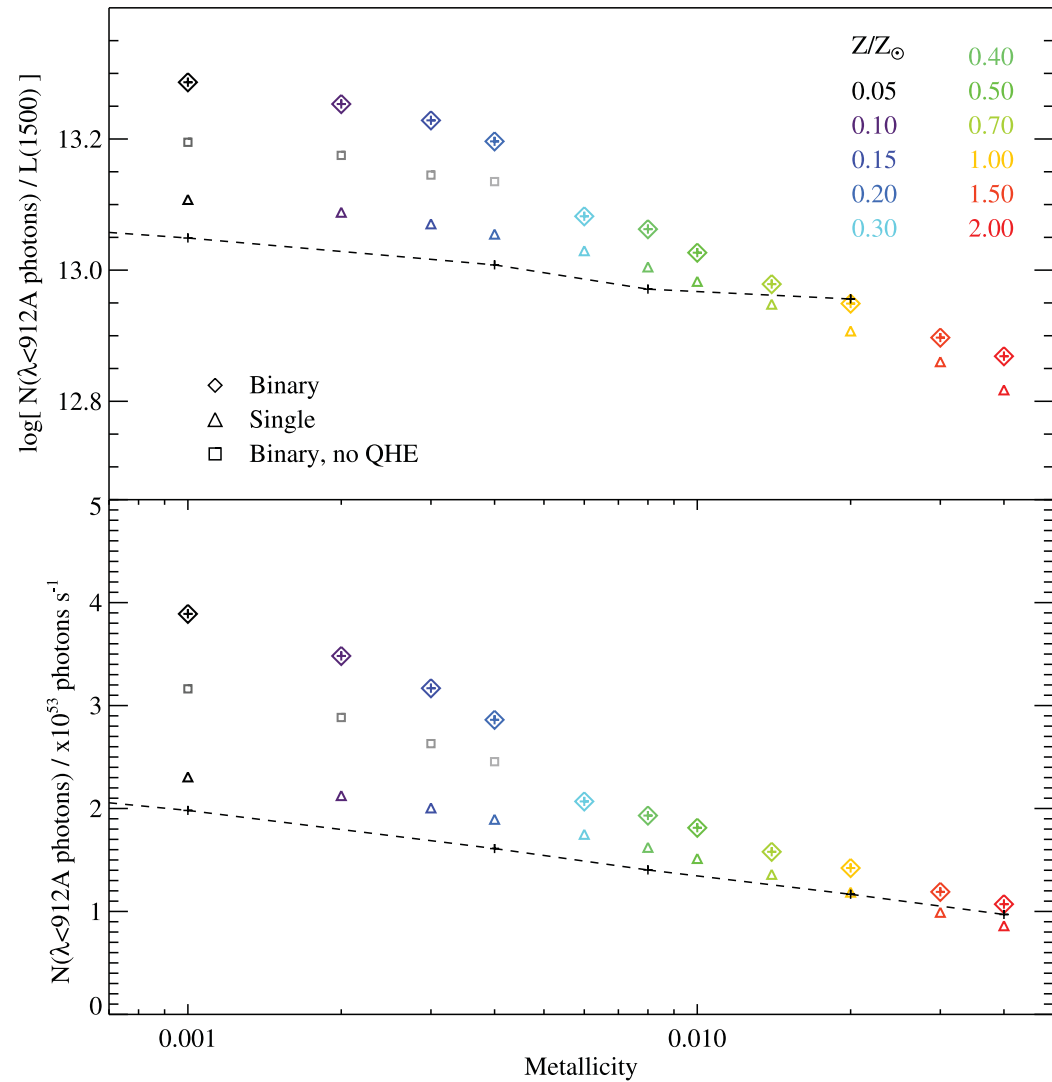
reionising the Universe – first stars? first galaxies?

effect of binary systems on ionizing photon flux



Moe et al. (2017)

strength of ionizing photons



Stanway et al. (2016)

■ Cosmic Dawn: The Real Moment of Creation

The screenshot shows a web browser window with the URL www.bbc.co.uk/programmes/b06b9tnx. The page features a navigation bar with links for Home, Episodes, Clips, Health Test FAQ, and Information and Support. The main content area includes a large image of a person walking through a forest with sunlight rays, a 'Watch now' button, and the title 'Cosmic Dawn: The Real Moment of Creation' (Episode 18 of 19). A 'Last on' section shows the broadcast date (Thu 10 Sep 2015, 23:45) and channel (BBC TWO SCOTLAND). A 'More episodes' section lists 'Which Universe Are We In?' (2014-2015) and 'Are Video Games Really That Bad?' (2014-2015). A 'See all episodes from Horizon' link is also present.